## **EXPECTED AND UNEXPECTED DEVELOPMENTS IN QUANTUM** COMPUTING

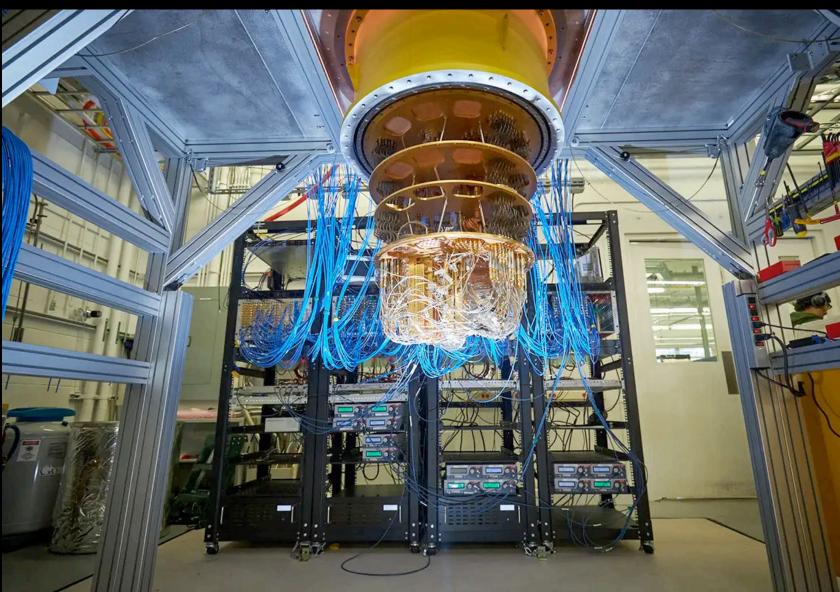
10/4/25

Joke title: Is this whole conference a waste of time?

Samuel Jaques



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Rocco Ceselin/Google



### **MAIN QUESTION**

When are quantum computers going to break RSA-2048? That is: when will they vindicate all the research at this conference?

1. Intro to Quantum computers 2. The "Business as (un)usual" path 3. Possible disruptions to that path

### OUTLINE

# **QUANTUM COMPUTERS** A quick introduction

## **Basics: Qubits**

A **qubit** is a device that holds **quantum data**, which can be  $|0\rangle$ ,  $|1\rangle$ , or any complex linear combination of the two (normalized to 1),

e.g. 
$$\frac{1}{\sqrt{2}} |0\rangle + \frac{1}{\sqrt{2}} |1\rangle$$
, or  $\frac{1}{2} |0\rangle - i\frac{\sqrt{3}}{2}|1\rangle$ 

 $1\rangle$ 

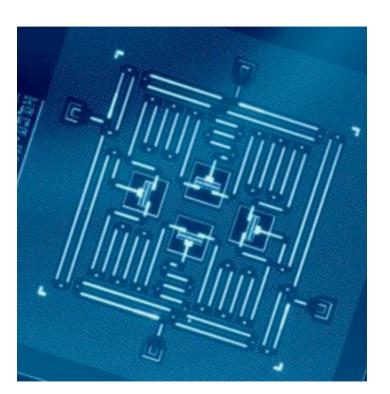




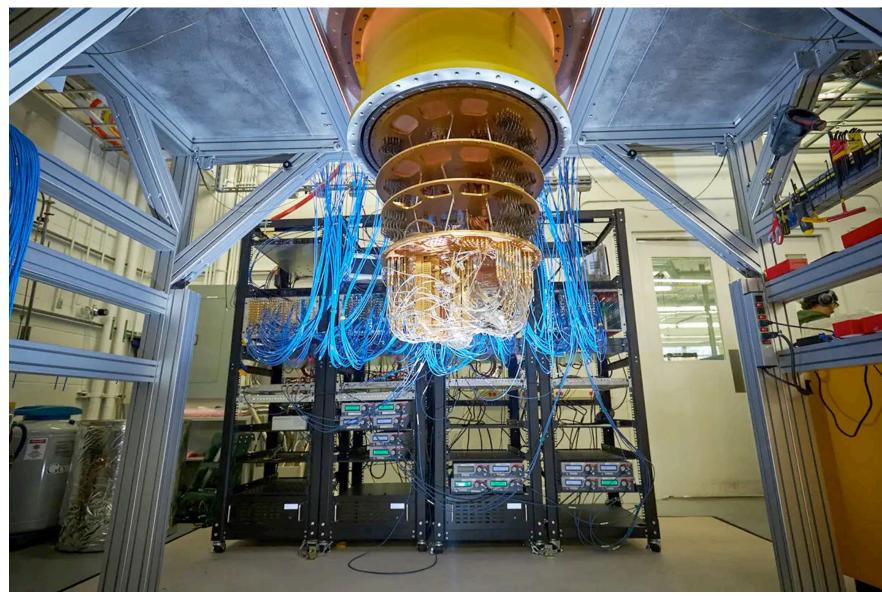
# **Qubit Types**

Any "two-level" quantum system can be a qubit:

### Superconducting qubits: A superconducting wire with current flowing in one direction or another



Jay M. Gambetta, Jerry M. Chow, and Matthias Steffen, 2017



Rocco Ceselin/Google

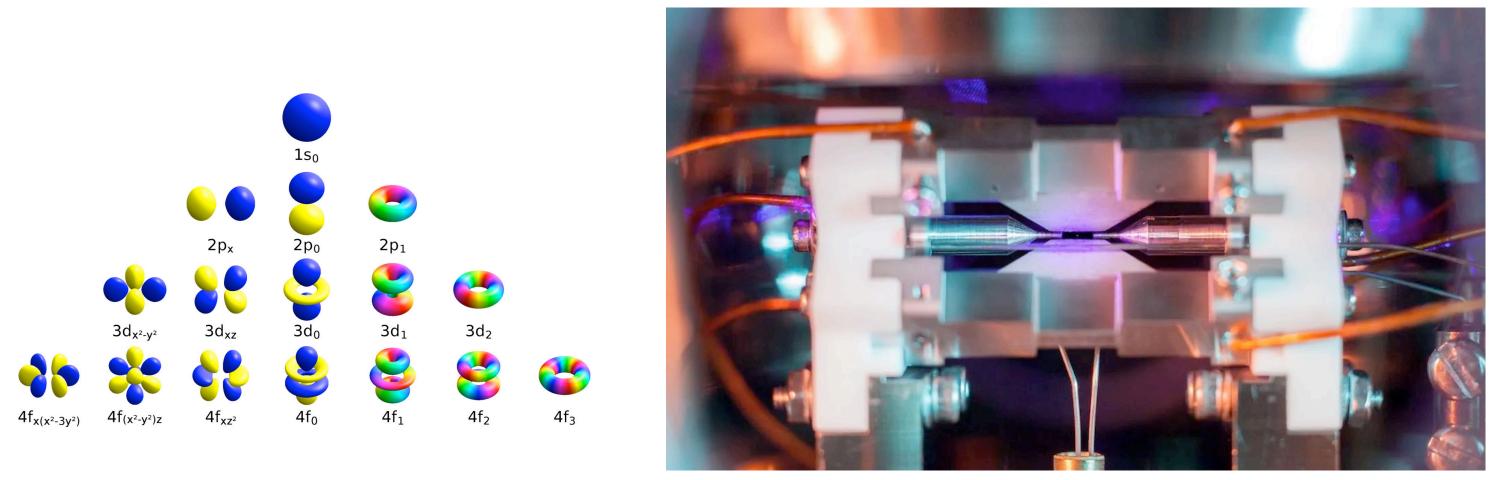




# **Qubit Types**

### Any "two-level" quantum system can be a qubit:

or low energy orbital



Wikipedia user Geek3

### **Trapped ion qubits**: an atom where electrons are either in a high

David Nadlinger



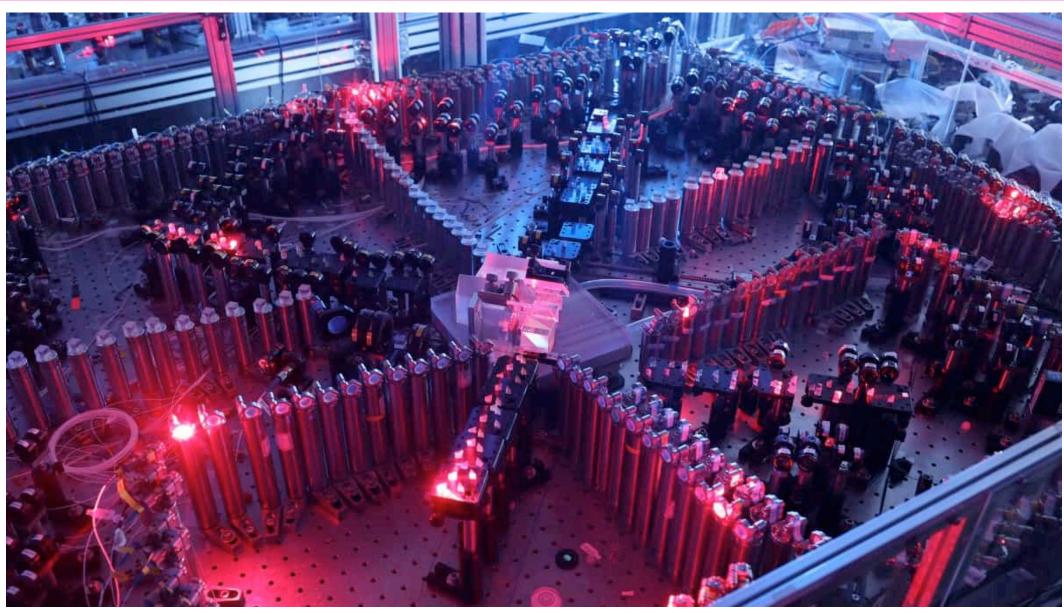
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# **Qubit Types**

Any "two-level" quantum system can be a qubit:

**Photonic qubits**: a photon that could be in one of two physical locations (e.g. fibre optic cables)



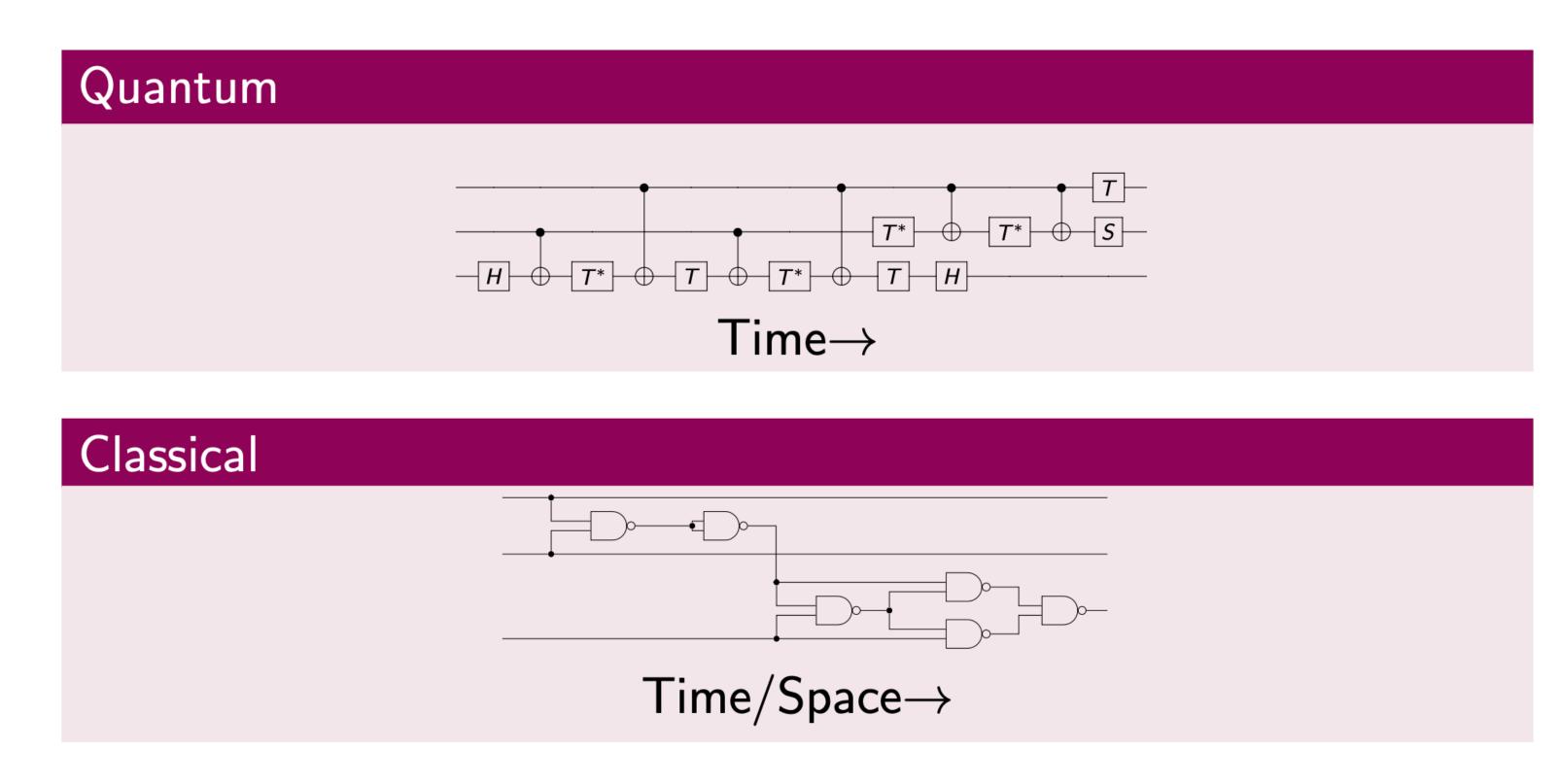
Chao-Yung Lu





## **Basics: Gates**

We manipulate the qubits with **gates**, which change the quantum data. Analogous to classical gates, but they are almost always a **process**, not a **device**.



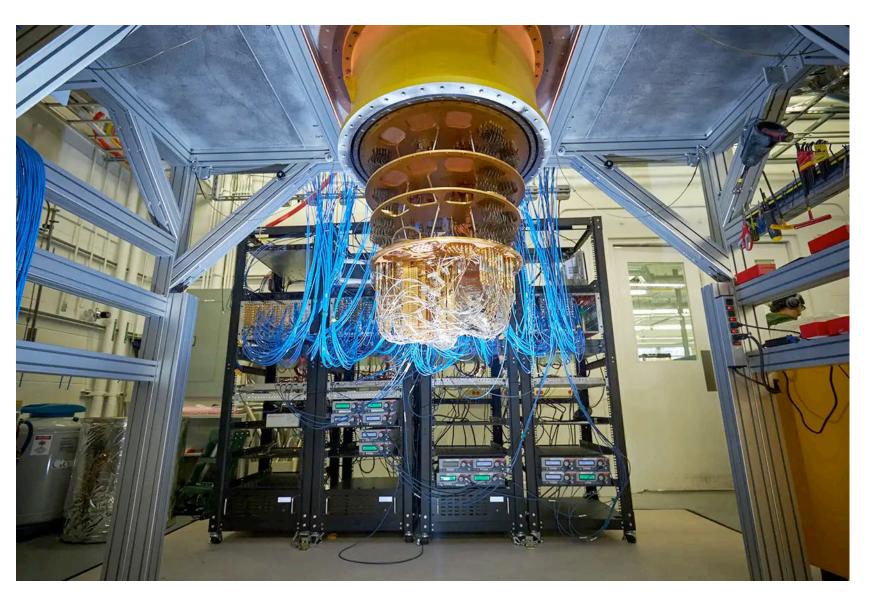




# **Basics:** Noise

Qubits are highly susceptible to noise. Noise is any uncontrolled process which modifies the quantum data.

- Classical noise is much easier to deal with: absorbing a small bit of energy won't flip a bit. For qubits, any unwanted interaction causes problems
- Qubits can have "bit flip errors" (similar to classical bit flip) but also "phase flip errors" (no classical analogue) or **any linear** combination of the two types



Rocco Ceselin/Google

$$|0\rangle \mapsto |1\rangle$$
  

$$|1\rangle \mapsto |0\rangle$$
  

$$|0\rangle \mapsto + |0\rangle$$
  

$$|0\rangle \mapsto - |1\rangle$$
  

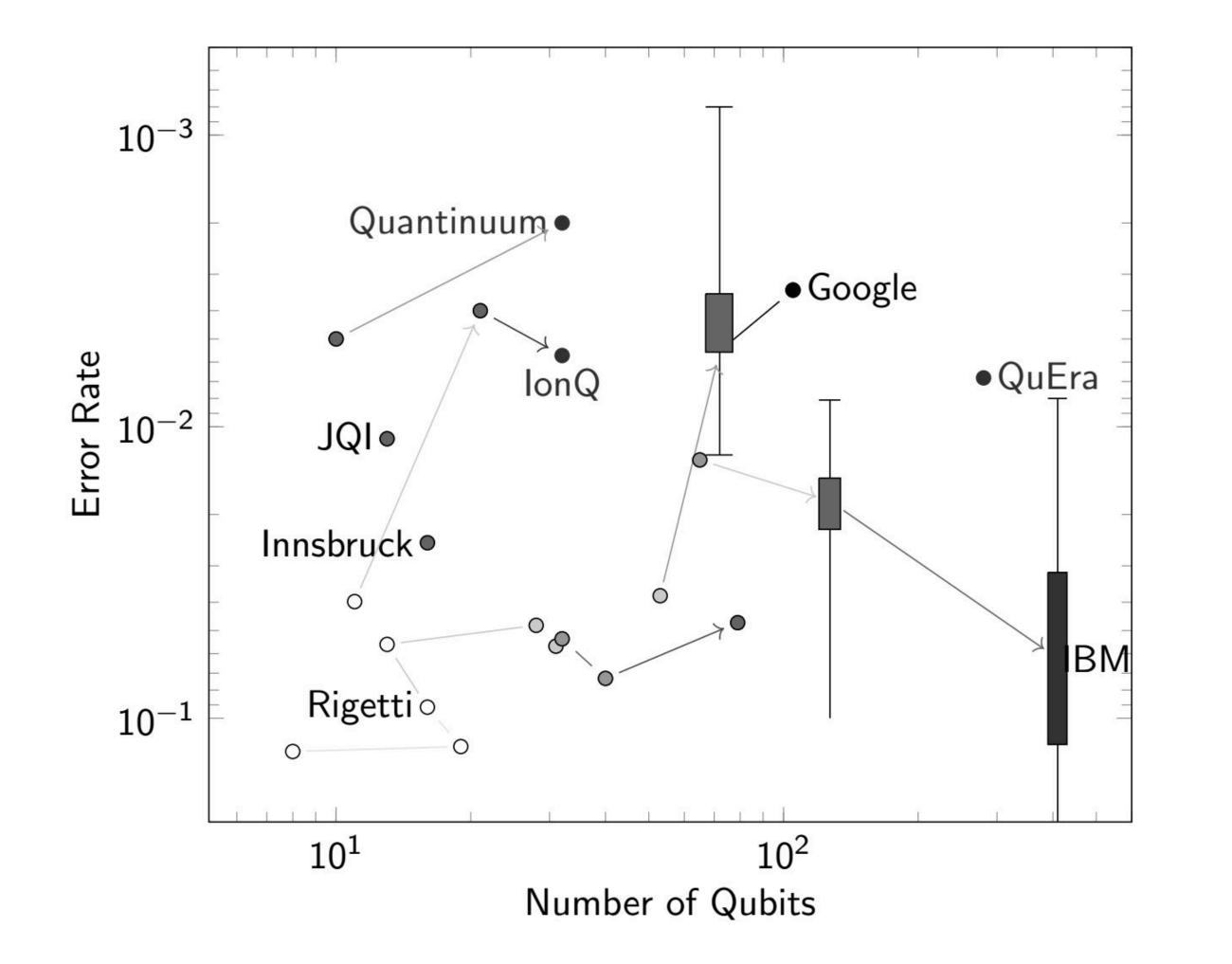
$$|0\rangle \mapsto - |1\rangle$$



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# **Quantum Computing Today**

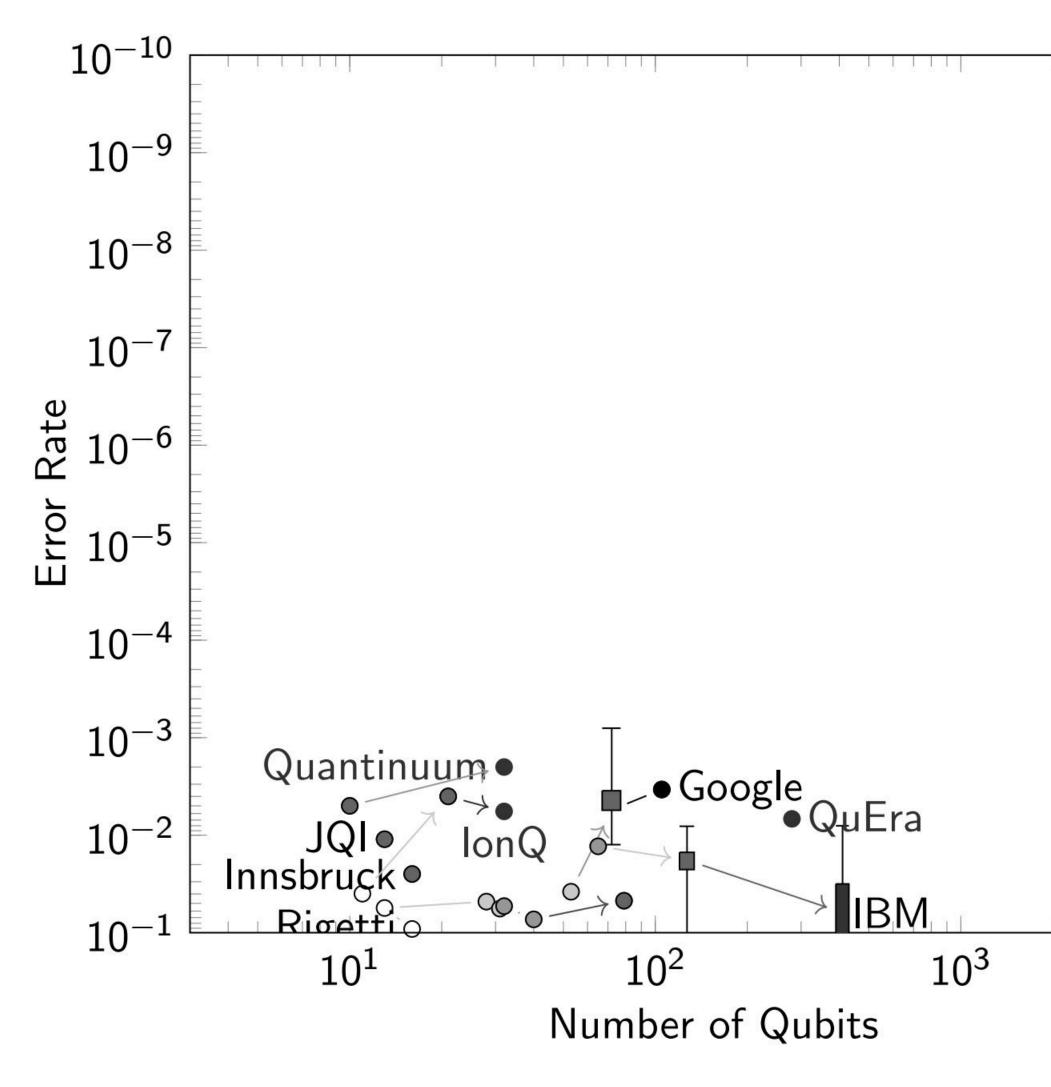


(I had to make dubious assumptions to compress "error rate" to a single number; this is not super precise)





# **Quantum Computing Today**















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  - Logical qubits: an abstraction representing the collection of qubits in a code that act like one high-fidelity qubit





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**1 qubit** with error rates a **billion** times better than today





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Basic assumption:

**1 qubit** with error rates a **billion** times better than today

Is much harder than

**1000 qubits** with error rates **ten** times better than today





# Surface Codes

- Most practical code at the moment
- Uses a 2-dimensional grid of qubits, each connected to its neighbours (easy to build)
- Suppresses errors exponentially in grid width
- Requires repeating cycles of measurement thousands or millions of times per second

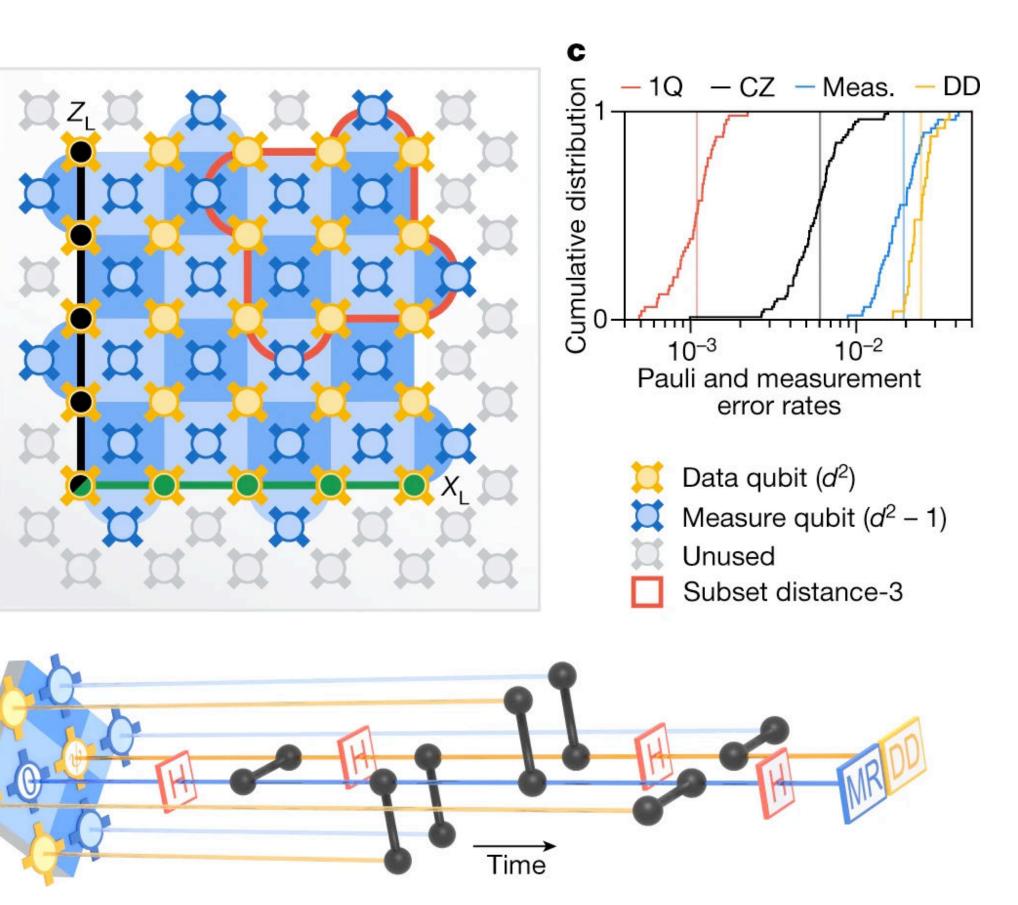


Diagram: Google Quantum AI



а

b



# Why surface codes?

- 1. Error detection is fast and simple
- 2. Physical connectivity is simple (2-d grid of nearest-neighbour connections)
- 3. We know how to compute on encoded quantum data
- 4. 1000:1 ratio of physical:logical qubits is good enough
- 5. Lots of work on optimizing computation in surface codes



а

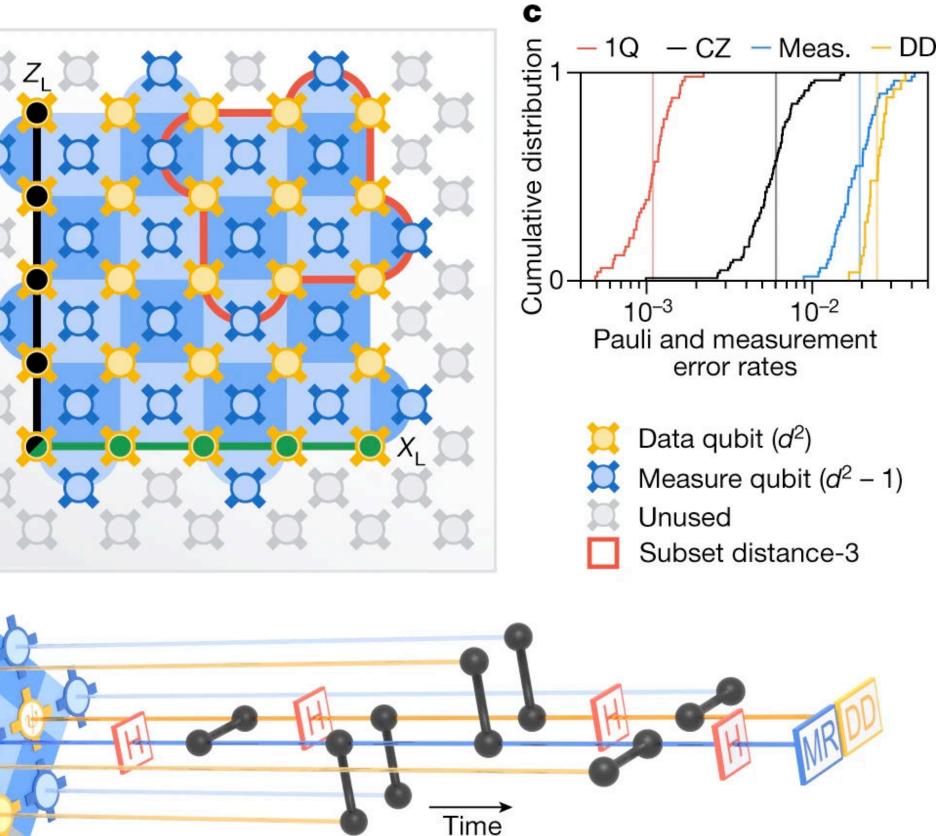
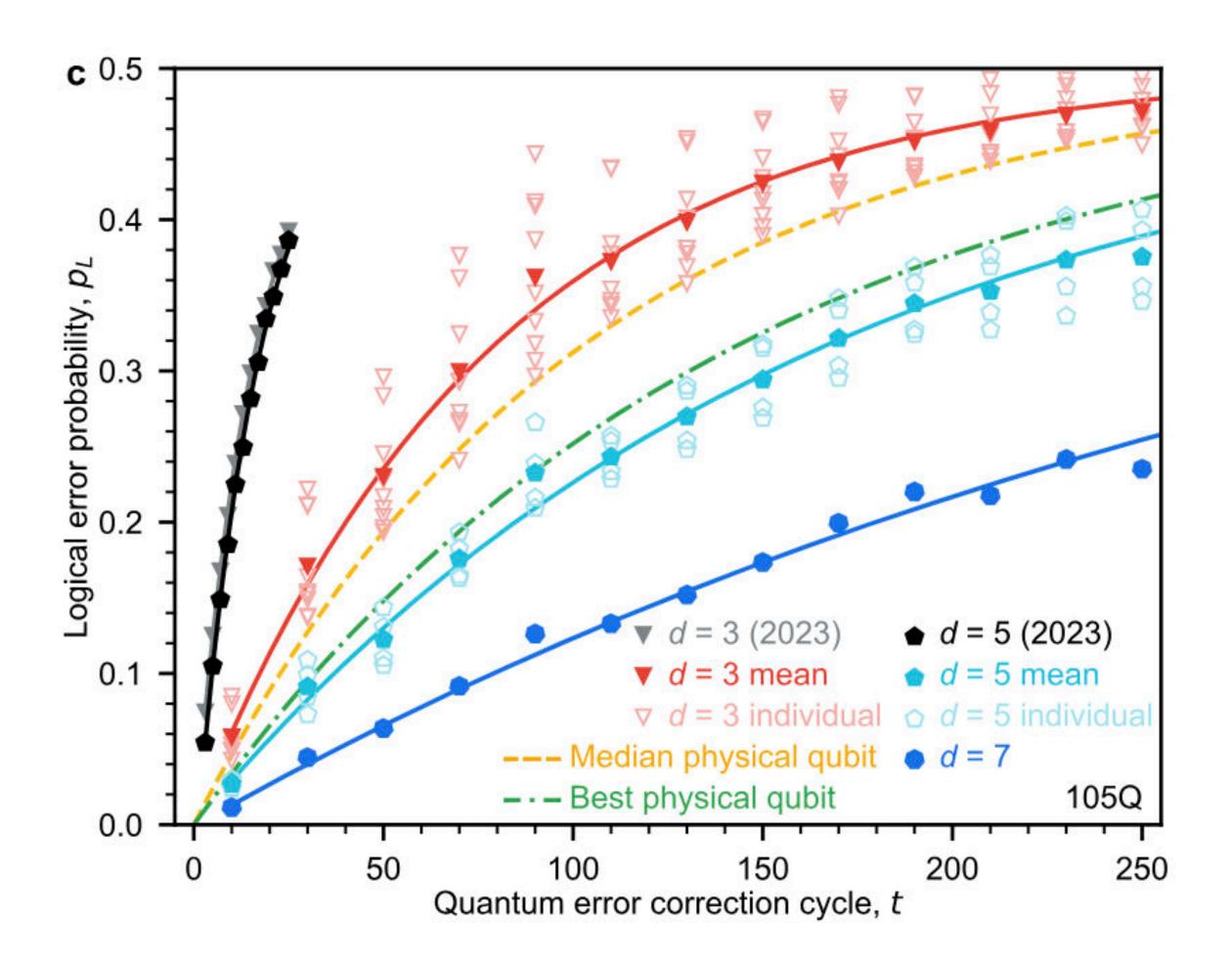


Diagram: Google Quantum AI





### Surface codes today



Breakthrough 2024 Experiment from Google Quantum AI:

- Error rate decreases as distance increases
- Logical qubit with smaller errors than physical qubits
- Real-time decoding at 1.1 µs cycle length





# Zuchongzhi 3.0: USTC's Quantum Computer

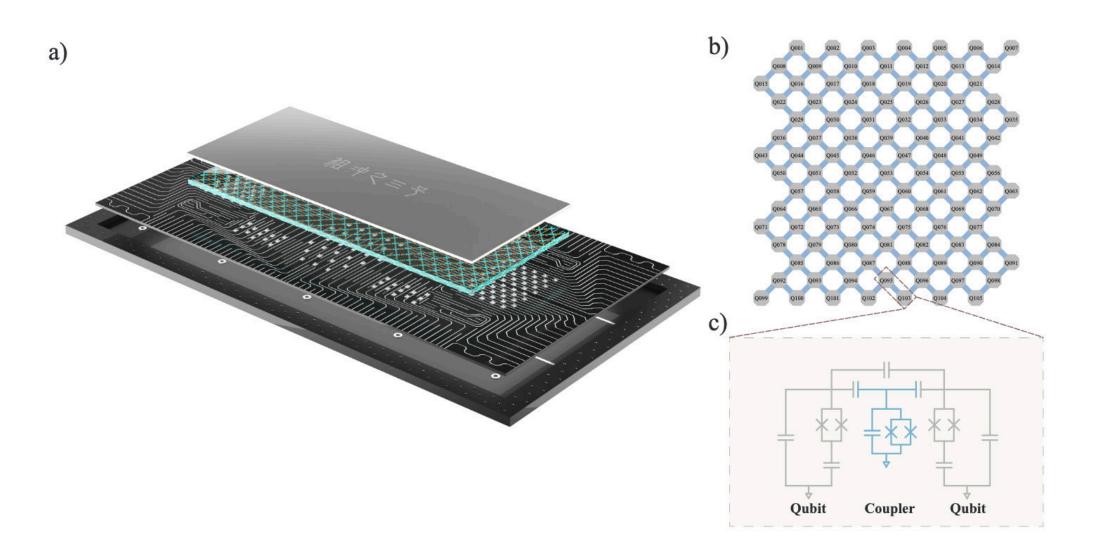
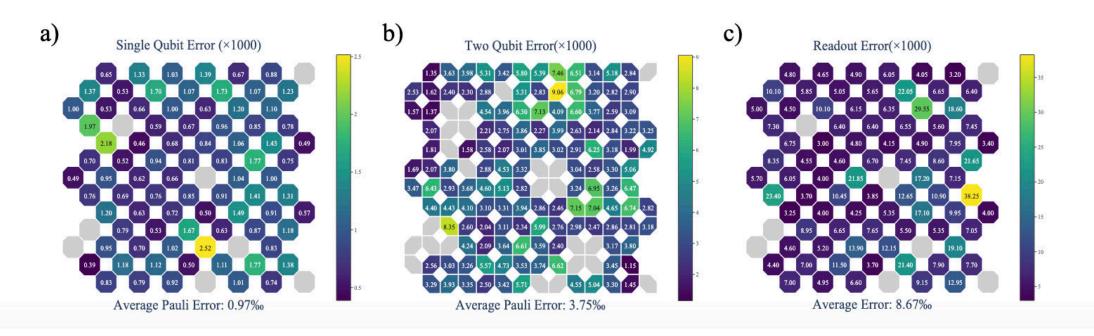


FIG. 1. Zuchongzhi 3.0 quantum processor. a) The illustration of the Zuchongzhi 3.0 quantum processor. The device consists of two sapphire chips integrated using a flip-chip technique. One chip integrates 105 qubits and 182 couplers, while the other is integrated with all the control lines and readout resonators. b) The topological diagram of qubits and couplers. Dark gray denotes qubits, light blue denotes couplers. c) Simplified circuit schematic of two qubits coupled via a coupler.

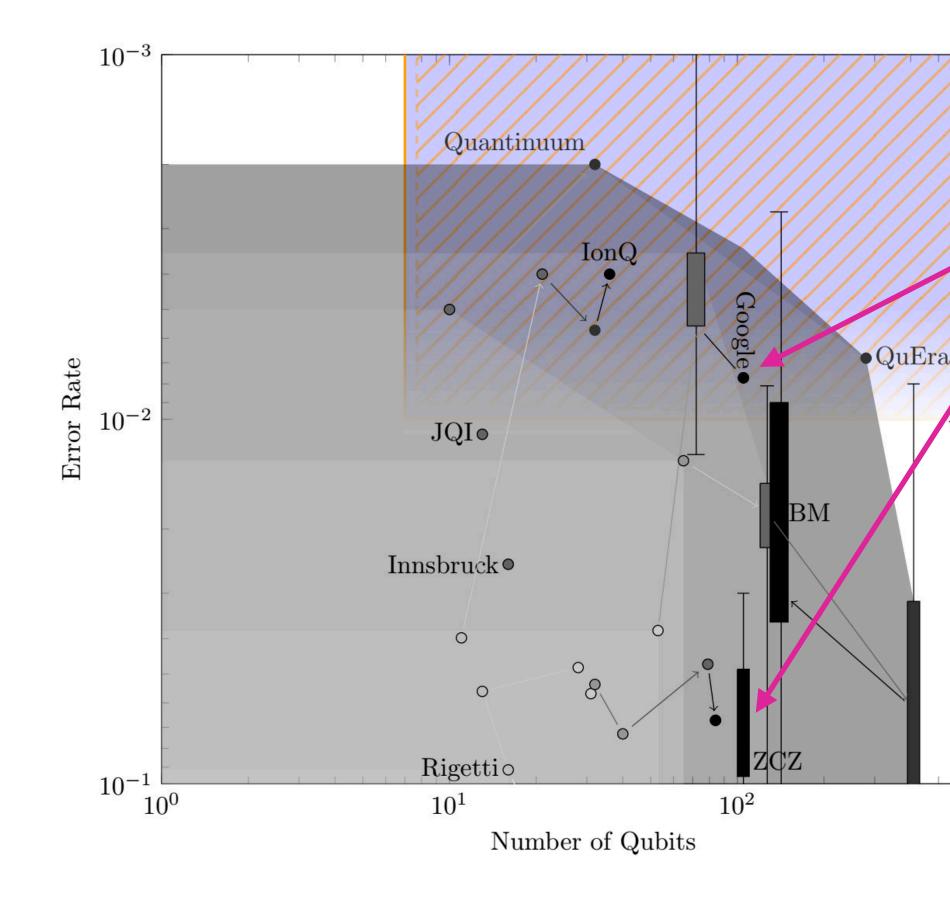


• From the abstract: "Our experiments with an 83-qubit, **32-cycle random** circuit sampling on Zuchongzhi 3.0 highlight its superior performance, achieving one million samples in just a few hundred seconds. This task is estimated to be infeasible on the most powerful classical supercomputers, Frontier, which would require approximately  $6.4 \times 109$  years to replicate the task. This leap in processing power places the classical simulation cost six orders of magnitude beyond Google's SYC-67 and SYC-70 experiments [Nature 634, 328 (2024)], firmly establishing a new benchmark in quantum computational advantage.





# Zuchongzhi 3.0: USTC's Quantum Computer



- ZuChongZhi 3.0 is a superconducting processor (like Google's "Willow")
- Not doing error correction
- Random circuit sampling is impressive but useless



We

 $10^{3}$ 

(CC)



## "Business As Usual" Path

- 1. Superconducting qubits get a bit better 2. The number of these qubits grows exponentially 3. Someone builds enough to factor (roughly 20 million) and we factor
- Engineering challenges:
  - The 200,000x increase in qubit counts • Dealing with massive error data throughput (100+ GB/second)

  - Real-time error correction
  - Building a large enough dilution fridge (or connections between fridges) Cosmic rays and other unexpected error events

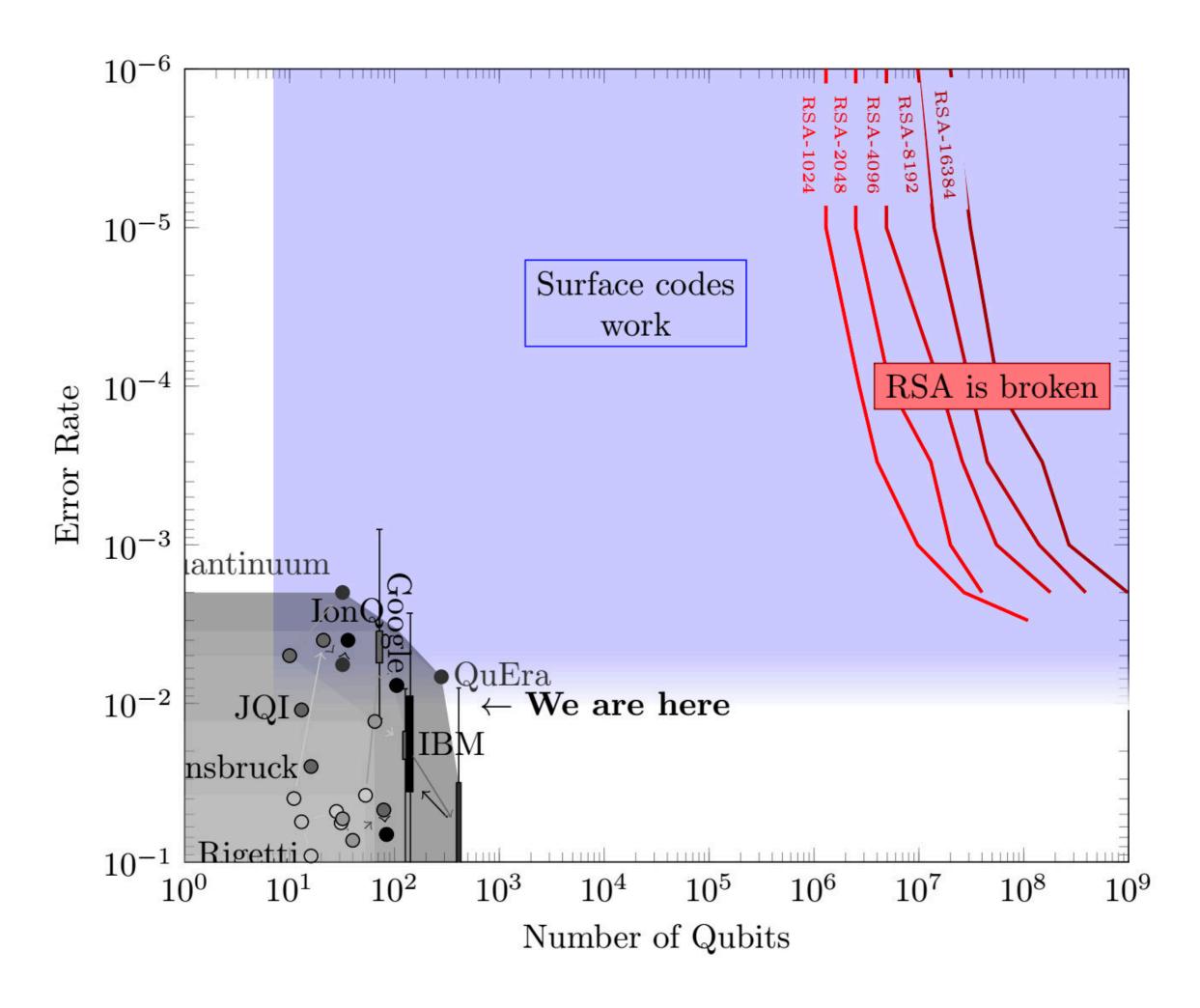
  - Other unknown challenges?
- For now assume these challenges are solved as they come up



19



## Time-to-break RSA: "Business as usual"



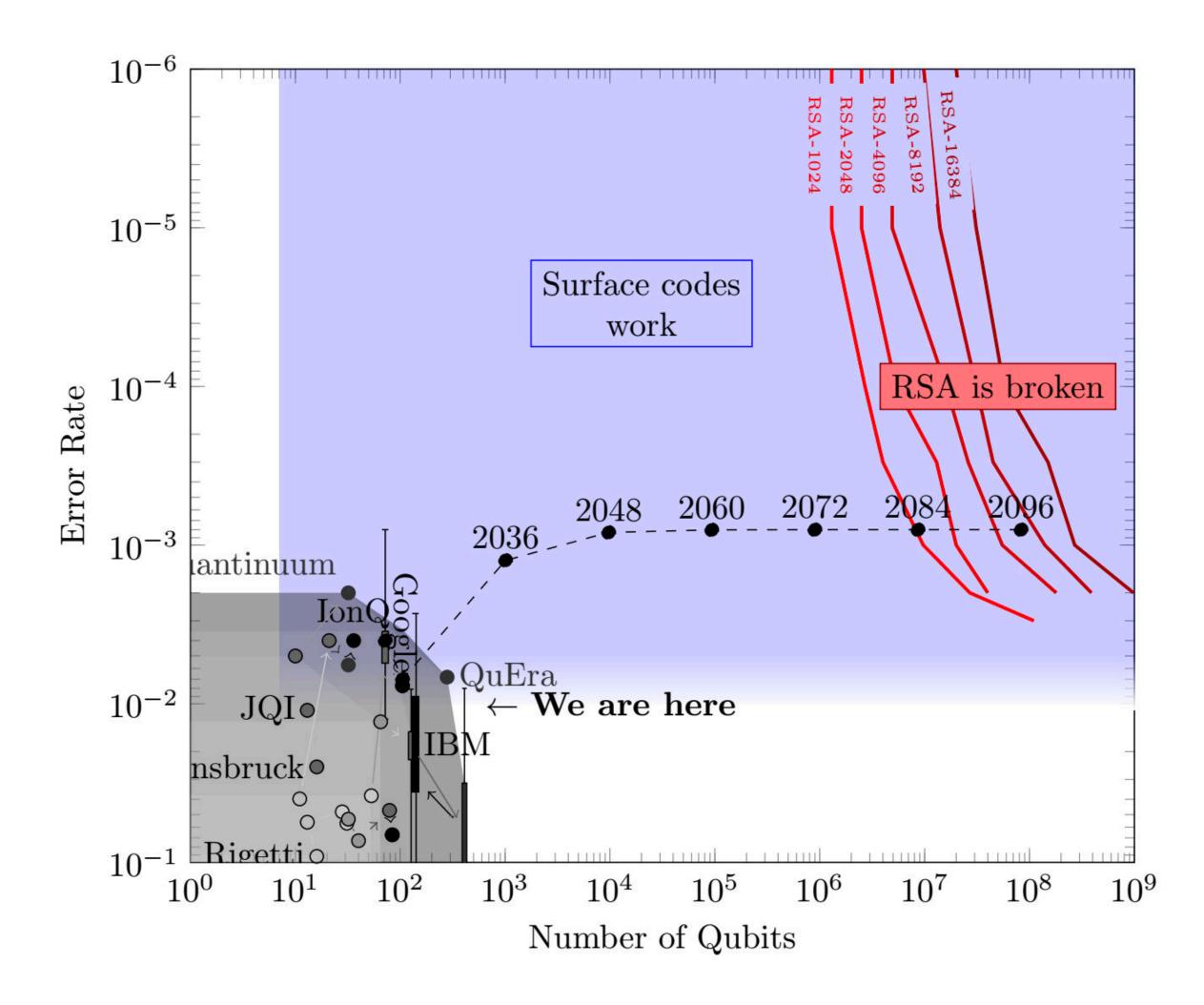
Google went from 72 qubits in 2022 to 105 in 2024 -> 45% increase in 2 years

At that rate...





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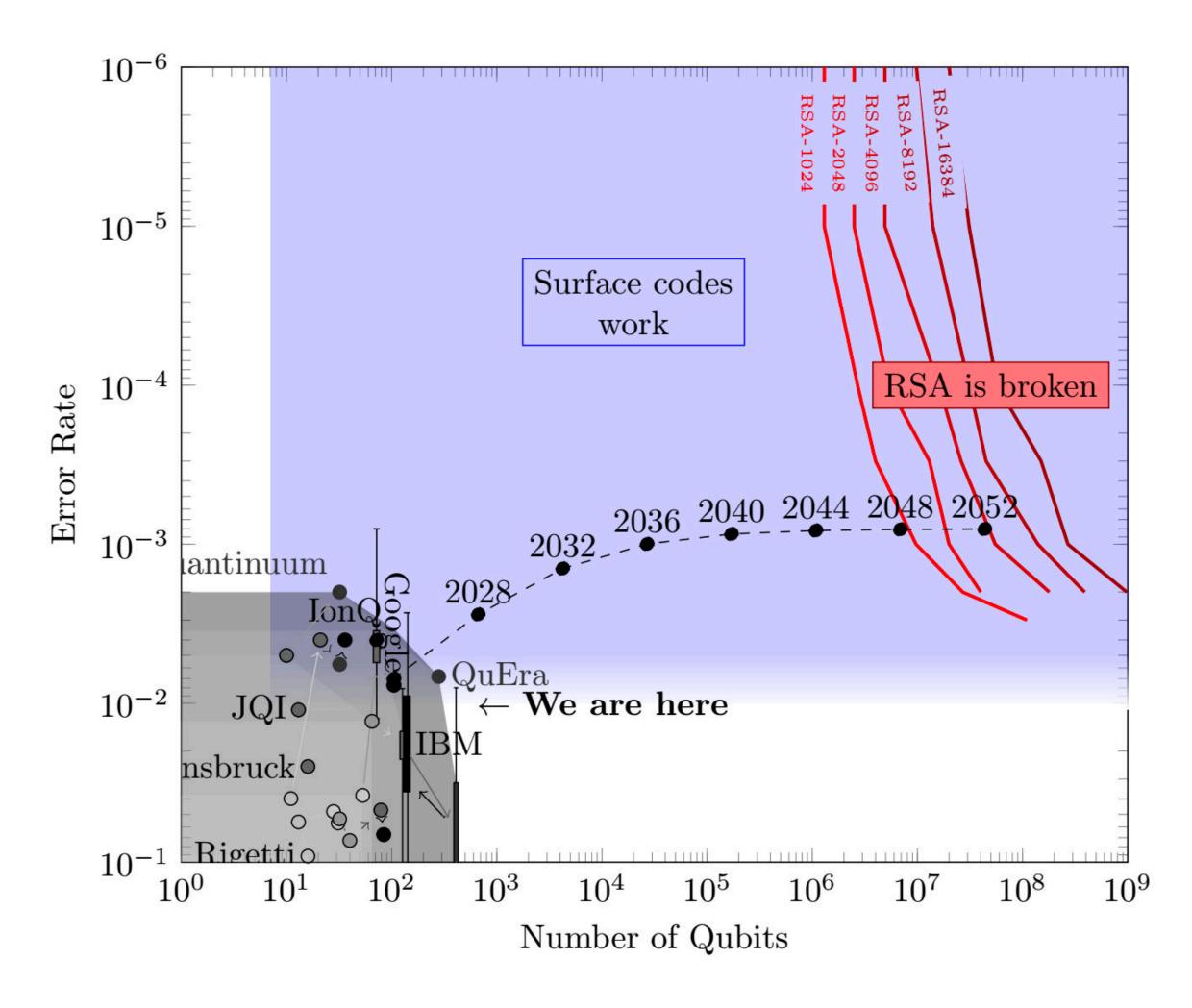
... RSA 2048 breaks in 2088

(Assuming physical error stalls at about 0.1%)





## Time-to-break RSA: "Business as usual"



To give them credit: they improved a lot of other factors in that 45% qubit increase.

What if quantum computers grow like Moore's law\*, doubling qubits every 1.5 years?

RSA-2048 breaks in 2052

\*up to technicalities in Moore's law





Assume qubits double every 1.5 years and error rate approaches 10<sup>-3</sup>:

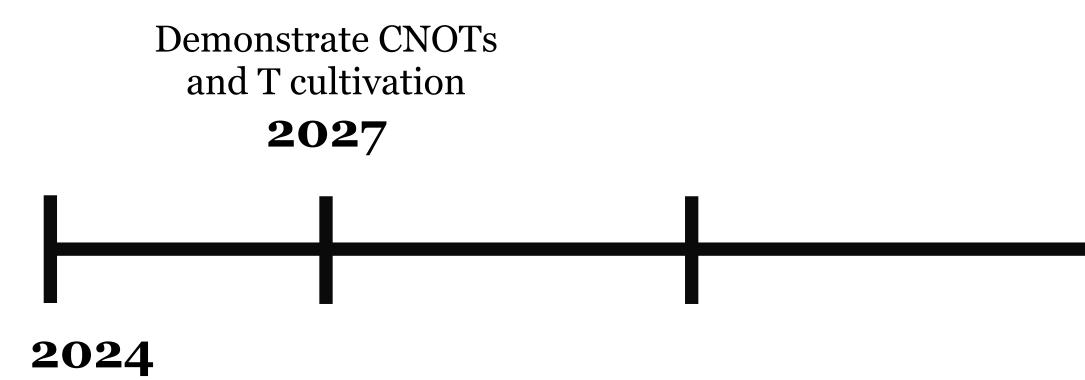


2024 1 (one) distance-7 Surface code logical qubit





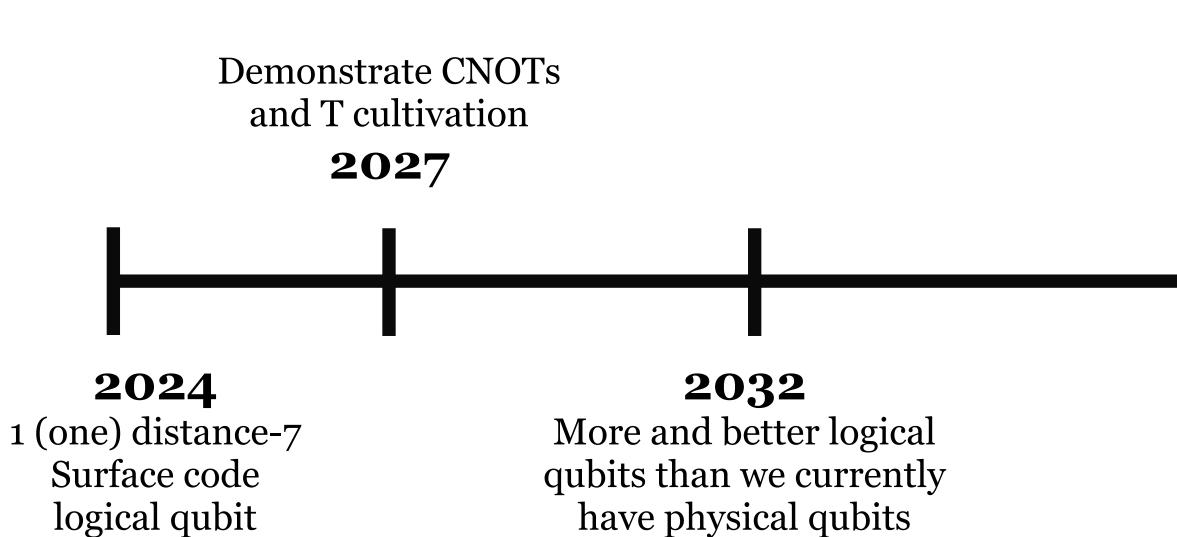
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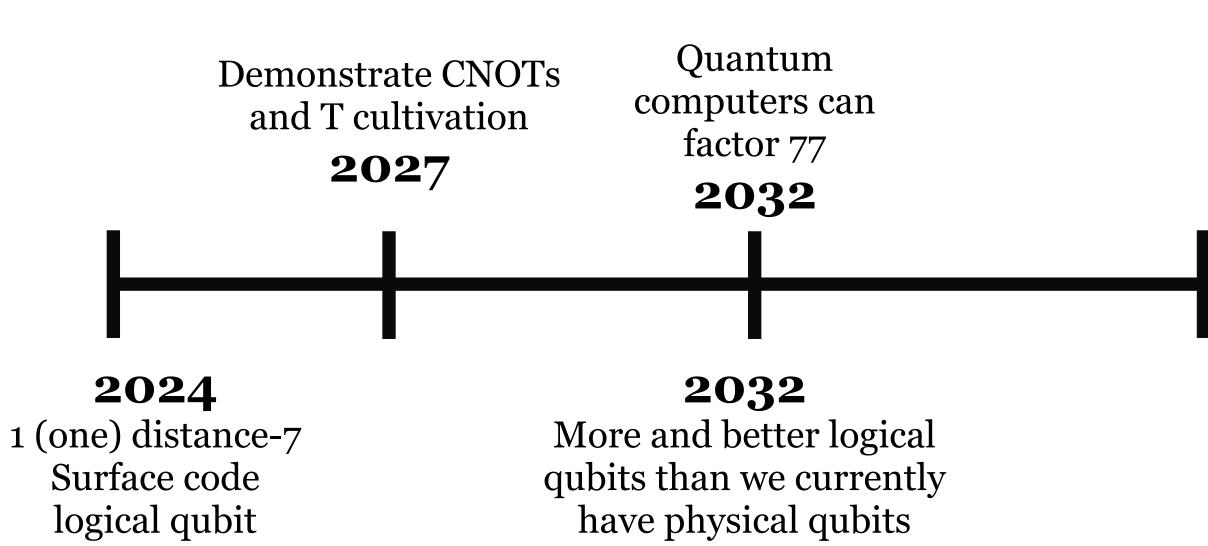






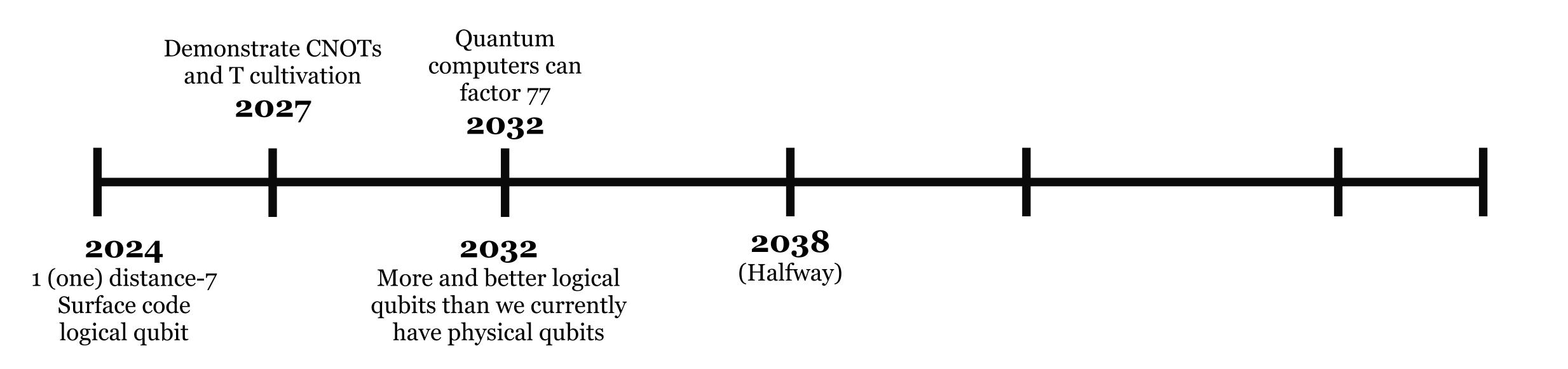






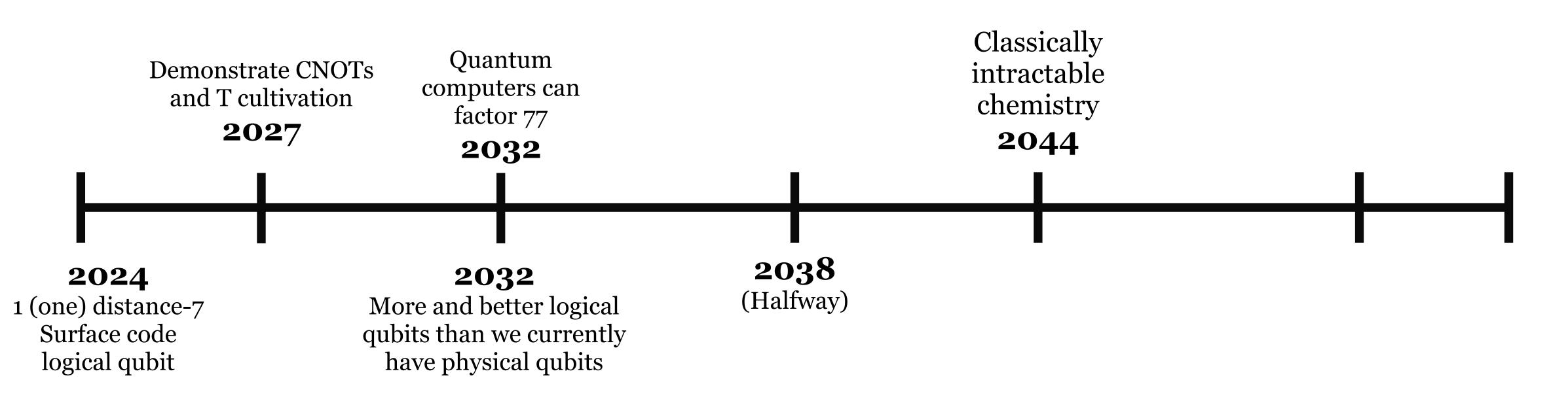








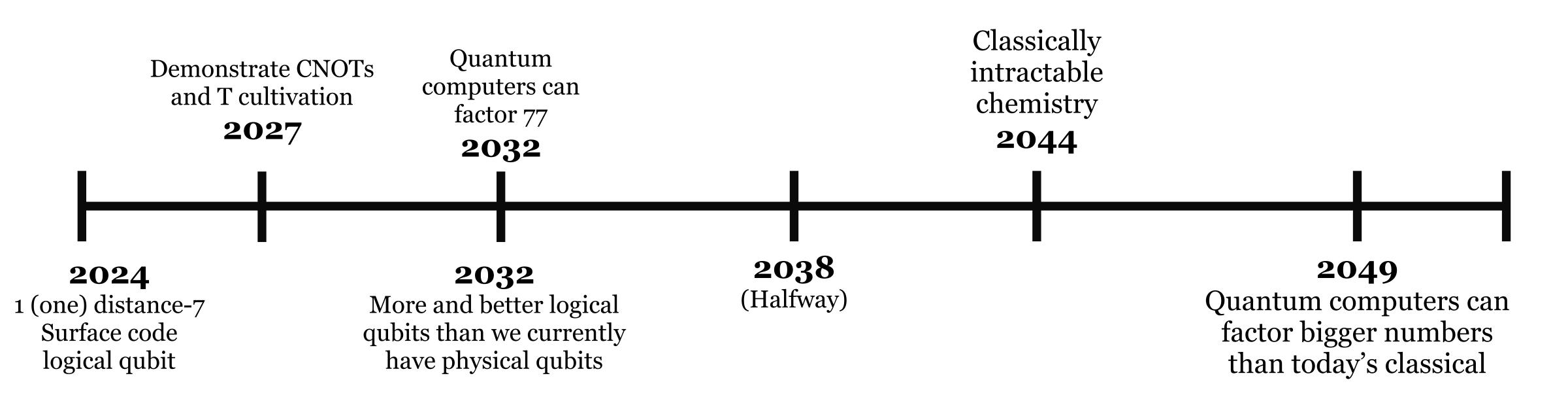












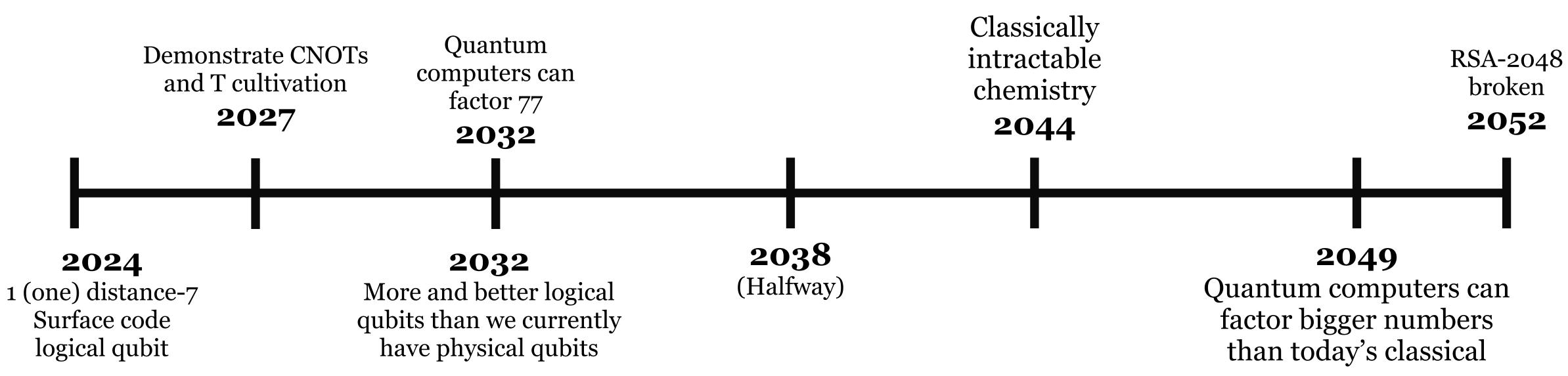






### Milestones

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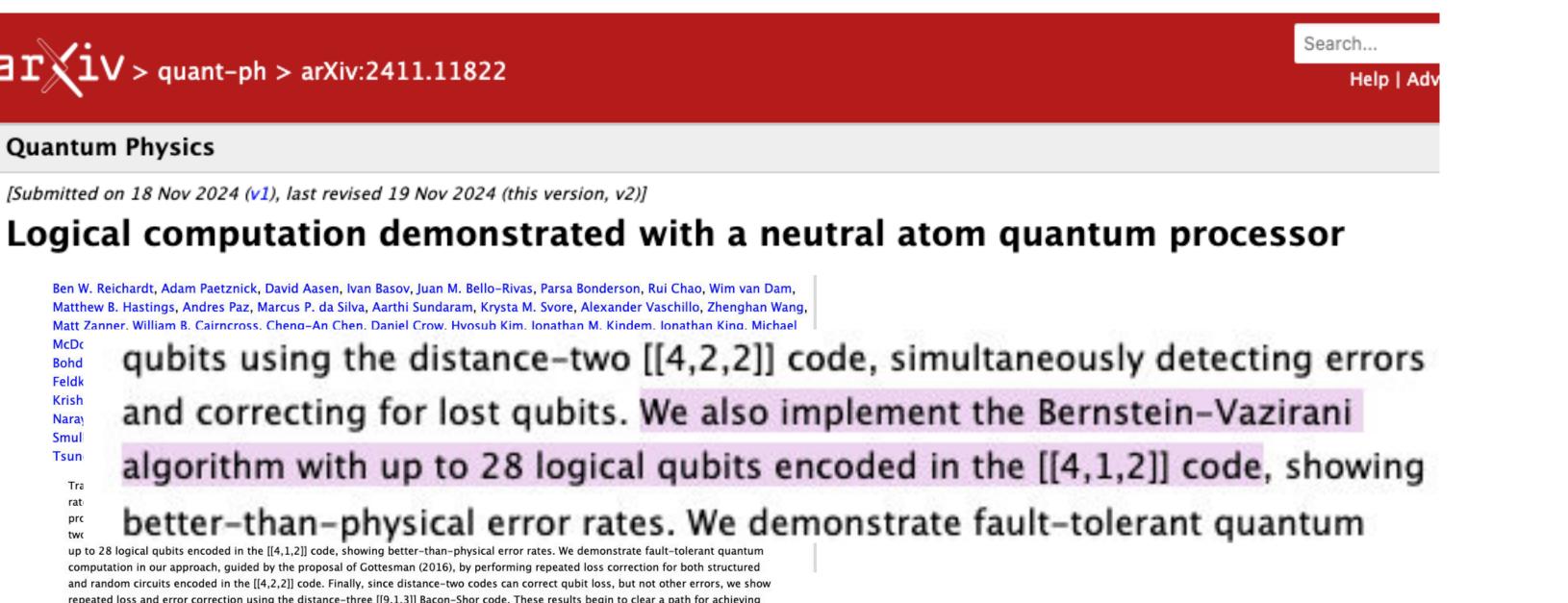






#### Quantum Physics

[Submitted on 18 Nov 2024 (v1), last revised 19 Nov 2024 (this version, v2)]



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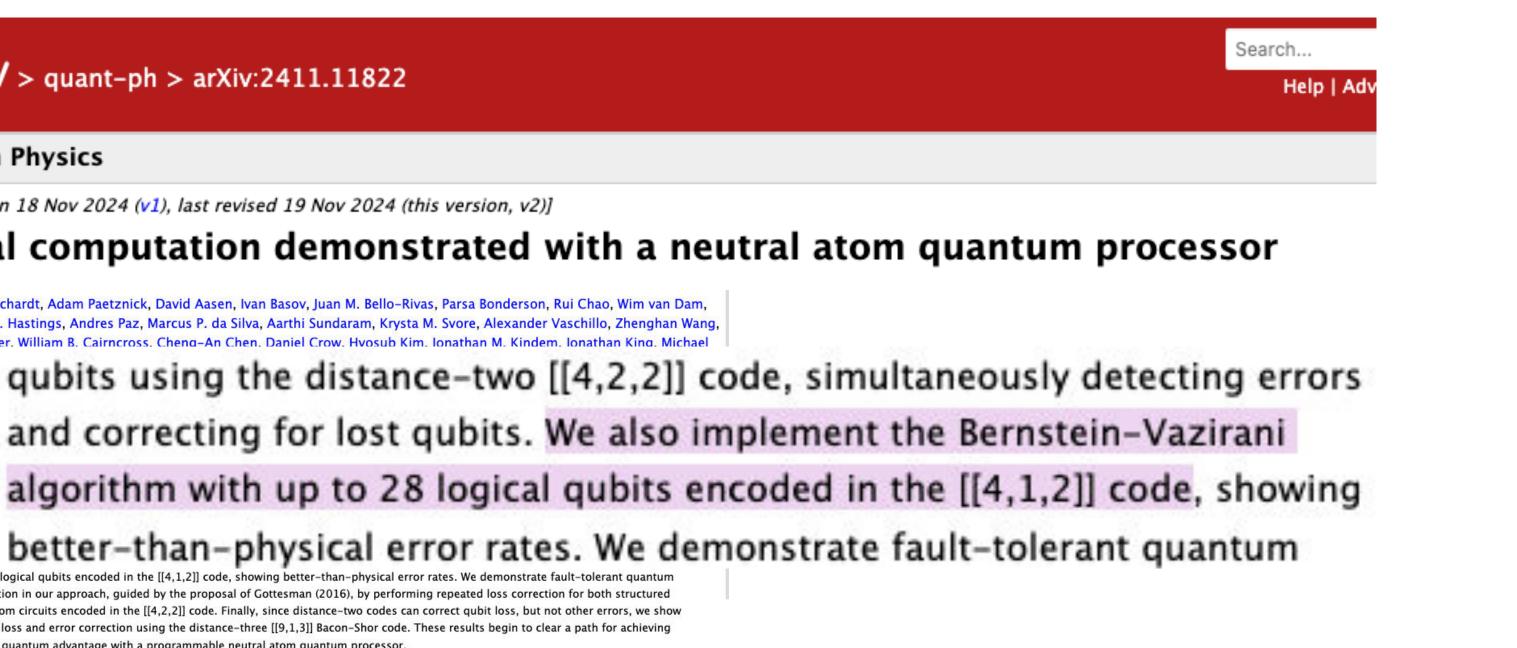
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McDo Bohd Feldk Krish Naray Smul Tsun Tra rat pro

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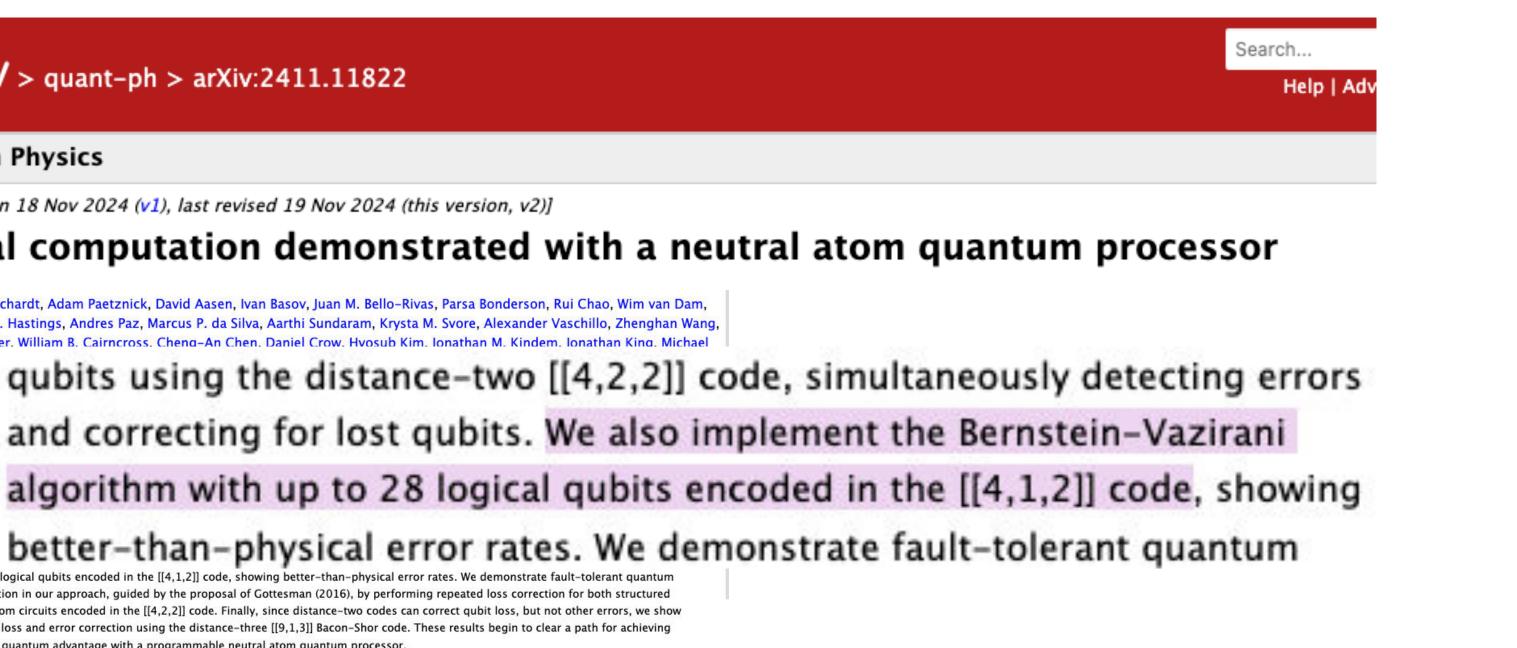
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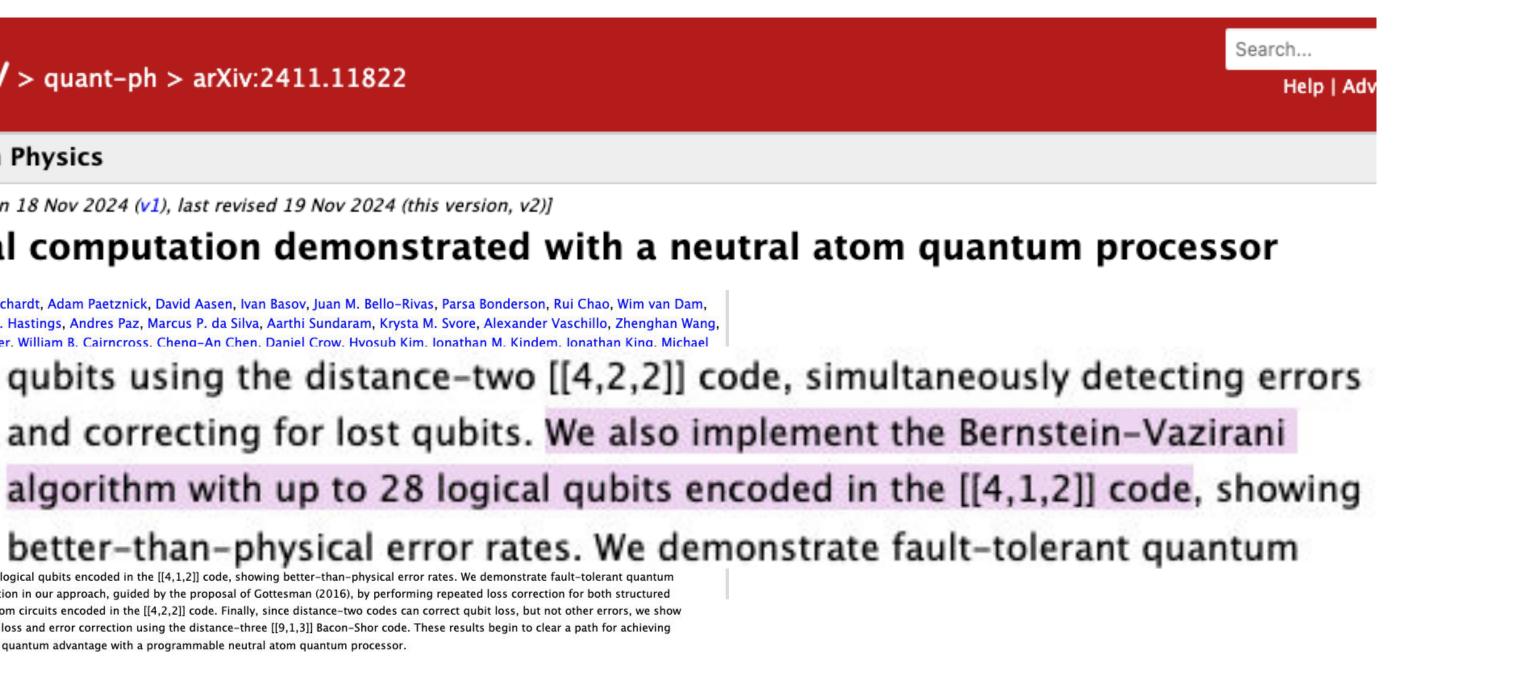
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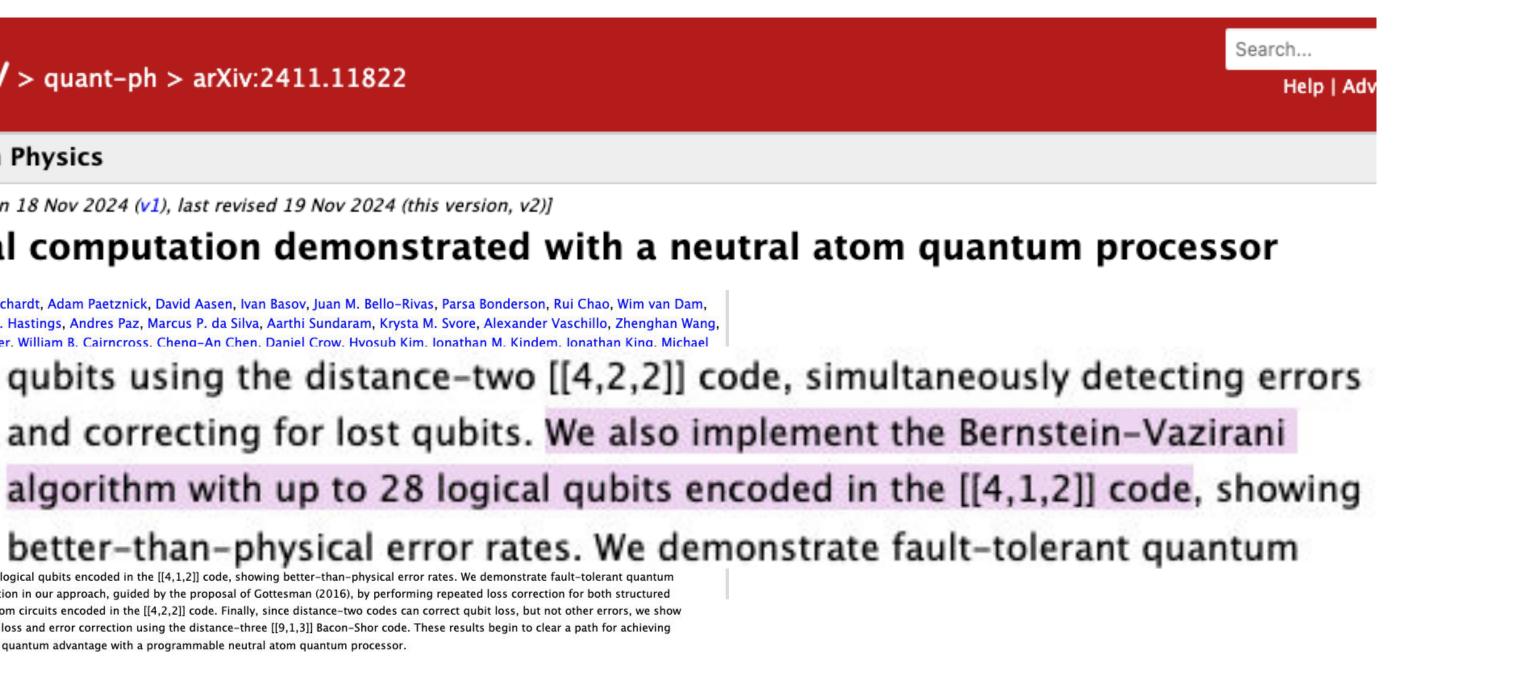
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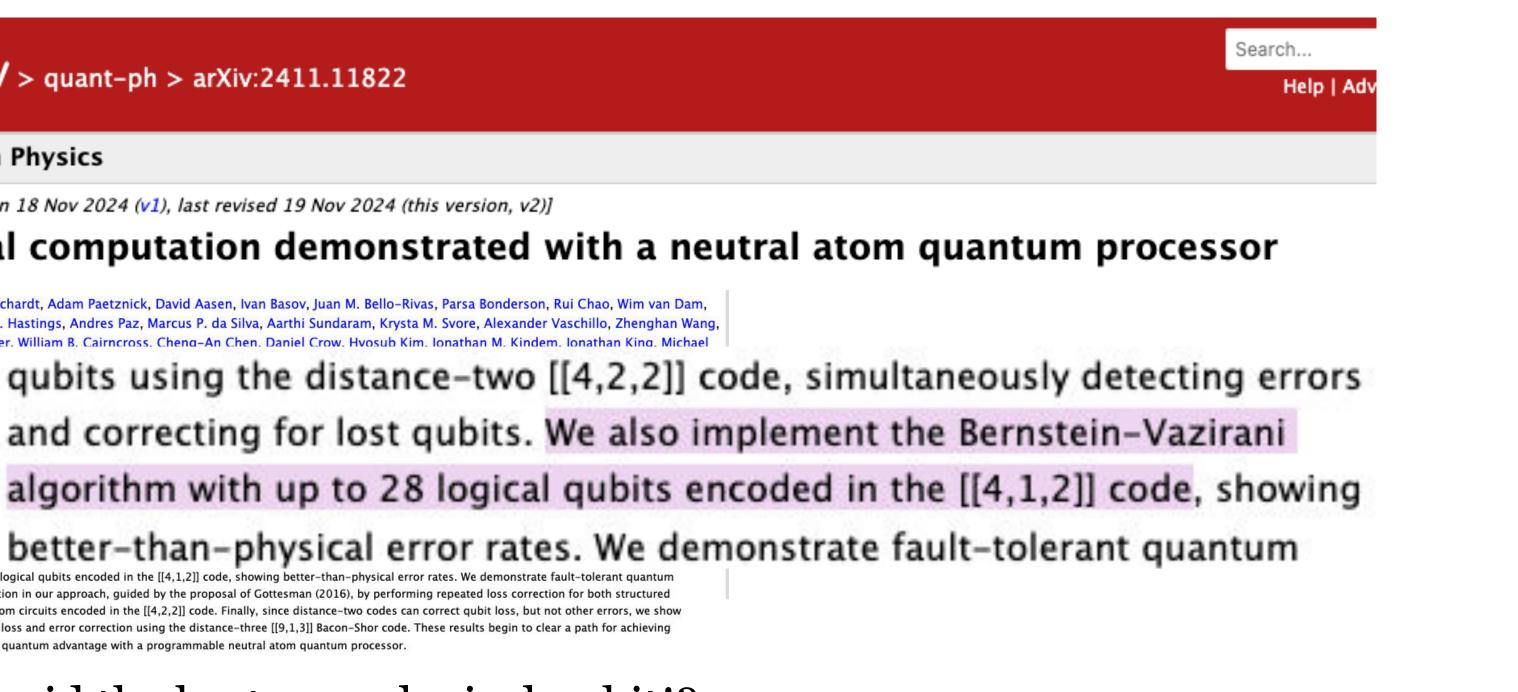
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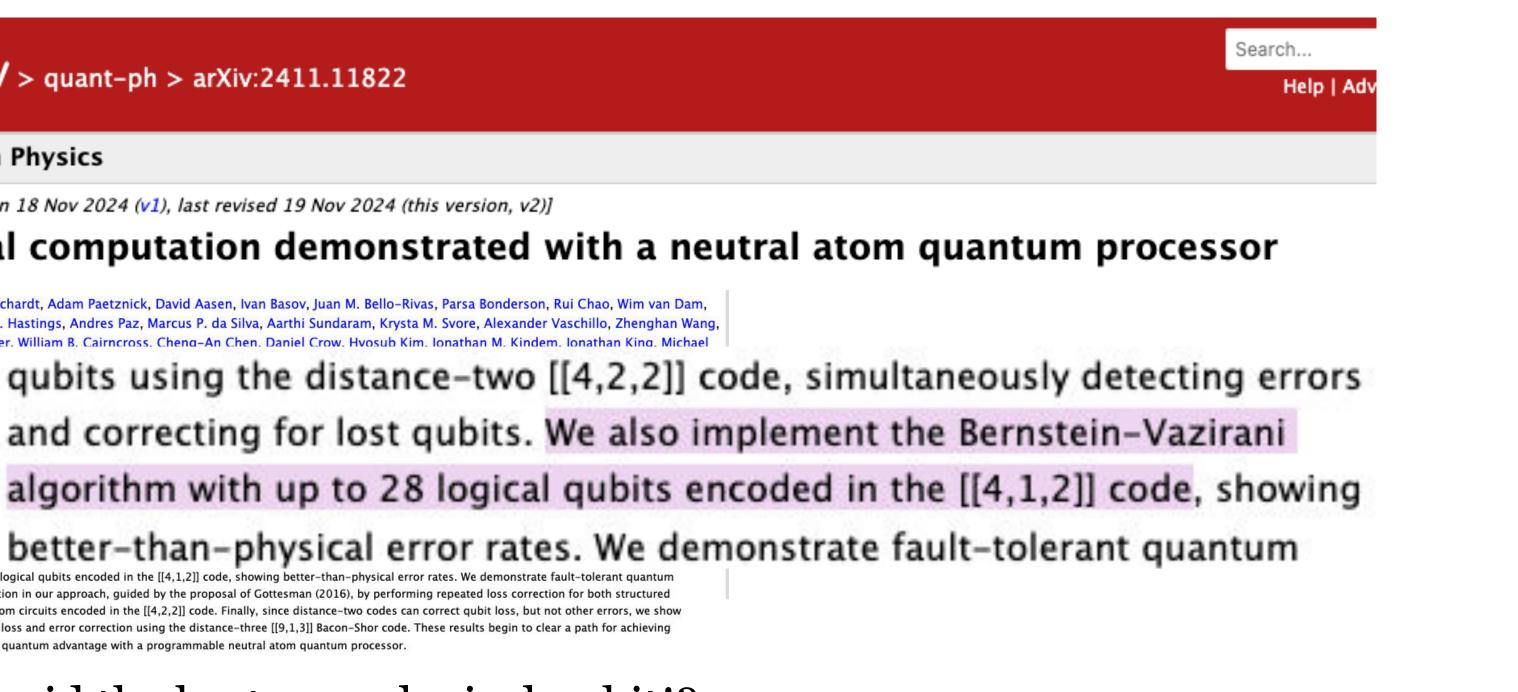
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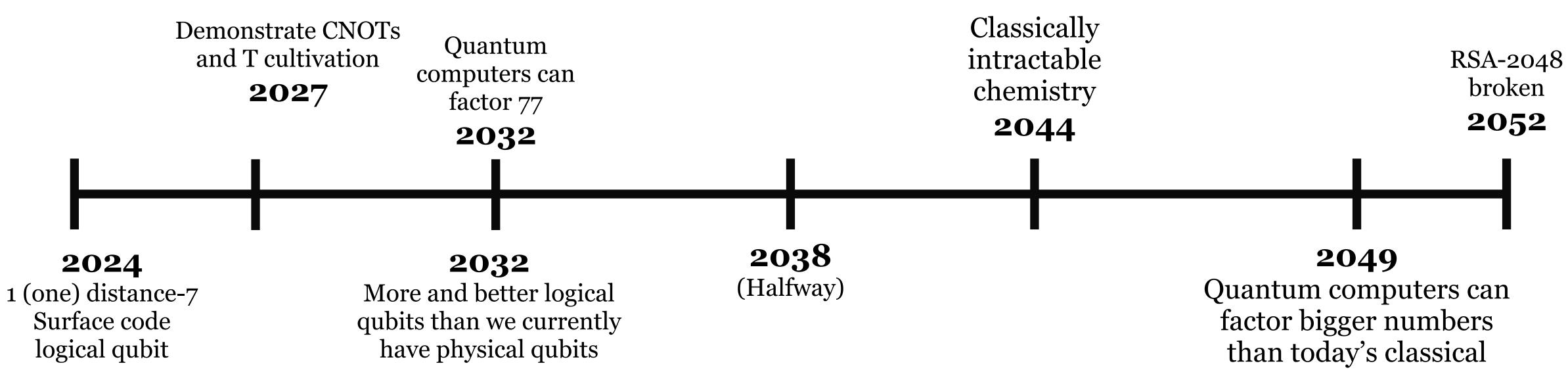






## **Changing The Timeline**

Assume qubits double every 1.5 years and error rate approaches 10<sup>-3</sup>:



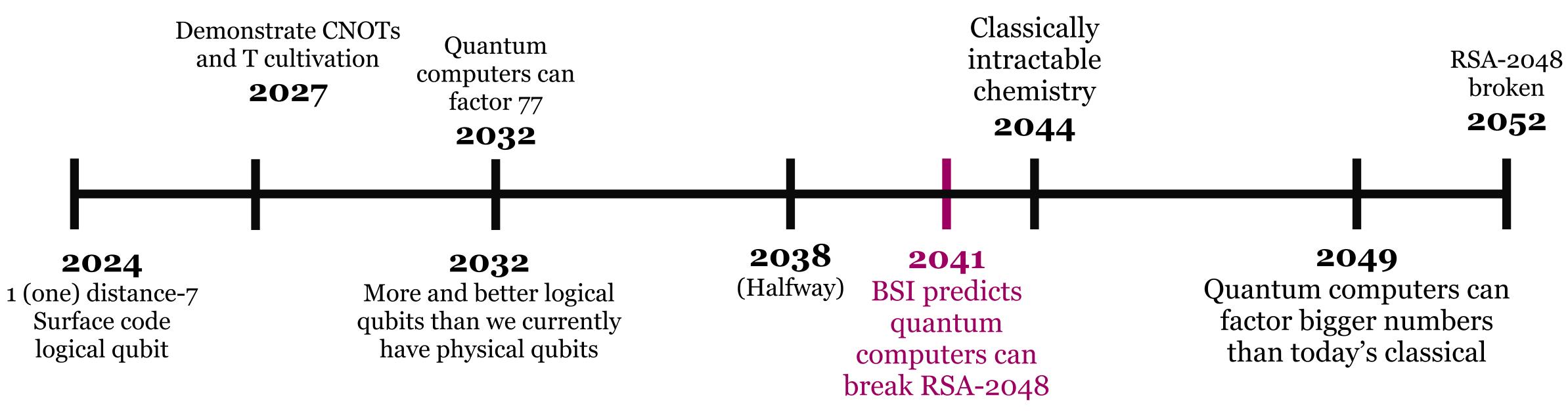






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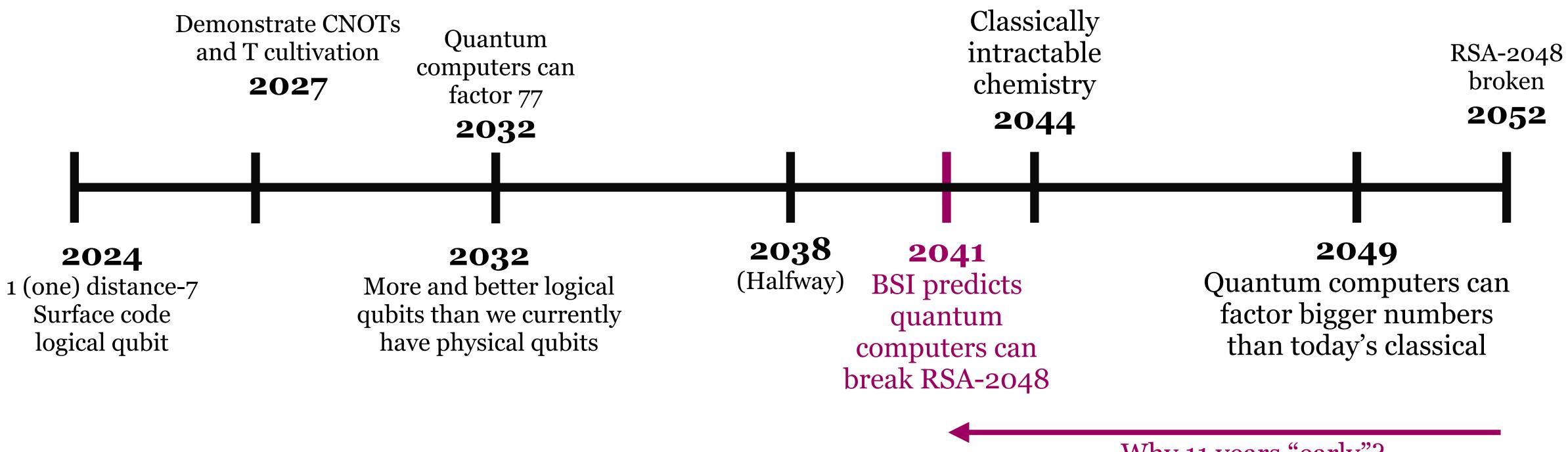






## **Changing The Timeline**

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#### **CHANGING THE TIMELINE**

1.	Better hardware
2.	Better codes
3.	Better algorithms
4.	Better implementations



### **1. Better Hardware**

Are superconducting qubits the "transistor" or the "vacuum tube"?



#### **Trapped Ions** Photo: David Nadlinger





#### It's still early days!





## **Topological Qubits**

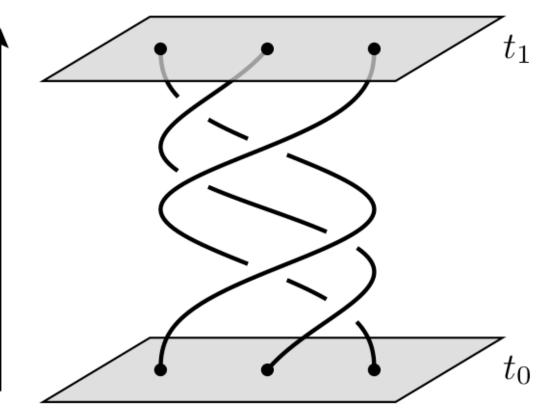
Idea: build a device where the qubit uses "Majorana" quasiparticles" which are inherently stable against noise

Rough idea: A "quasiparticle" is when many particles interact in way that looks mathematically like another particle

E.g.: waves on water

Majorana quasiparticles involve many "real" particles so a lot of the real particles must suffer noise to cause noise in the quasiparticle





**Diagram: Simon Burton** 





## **Topological Qubits**

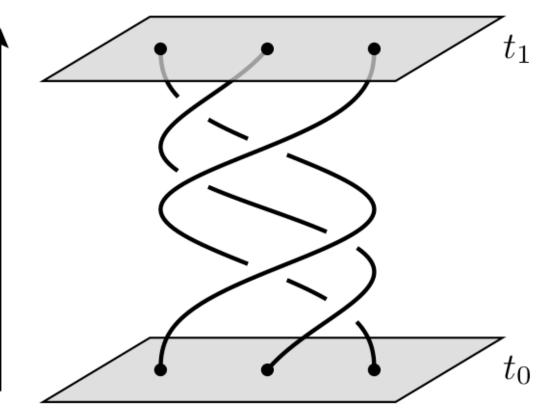
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quantum computing. It is an indium arsenide-aluminium hybrid device that admits superconductivity at low temperatures, and shows some signals of hosting boundary Majorana zero modes.<sup>[2][non-primary source needed]</sup> Majorana zero modes have the potential

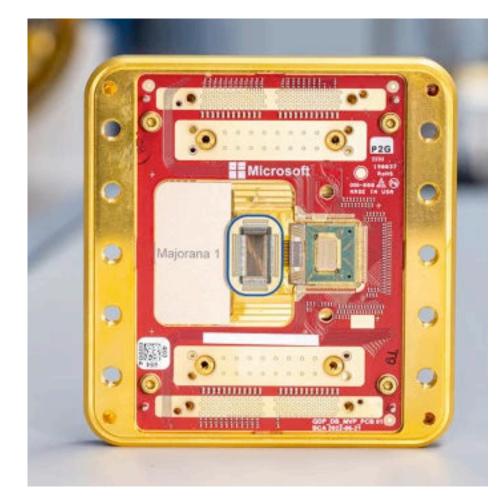


Photo: John Brecher





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NEWS 19 February 2025



#### Microsoft claims quantumcomputing breakthrough – but some physicists are sceptical





Photo: John Brecher





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## nature

#### Microsoft claims c nature portfolio computing breakt **Peer Review File**

#### some nhysicists ar

In my opinion, these experiments are very interesting and certainly relevant for the condensed matter community working on topological superconductors and Majorana states. What I do NOT like is the way the article is written which, sometimes subtly and sometimes more crudely, uses a language and wording that at all times leads the reader to think that we are dealing with a measurement that demonstrates parity in a topological qubit based on Majorana states. The examples are er many and here I highlight only a few:







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#### Microsoft claims c nature portfolio computing breakt **Peer Review File**

#### some nhysicists ar

In my opinion, these experiments are very interesting and certainly relevant for the condensed matter community working on topological superconductors and Majorana states. What I do NOT like is the way the article is written which, sometimes subtly and sometimes more crudely, uses a language and wording that at all times leads the reader to think that we are dealing with a measurement that demonstrates parity in a topological qubit based on Majorana states. The examples are er many and here I highlight only a few:



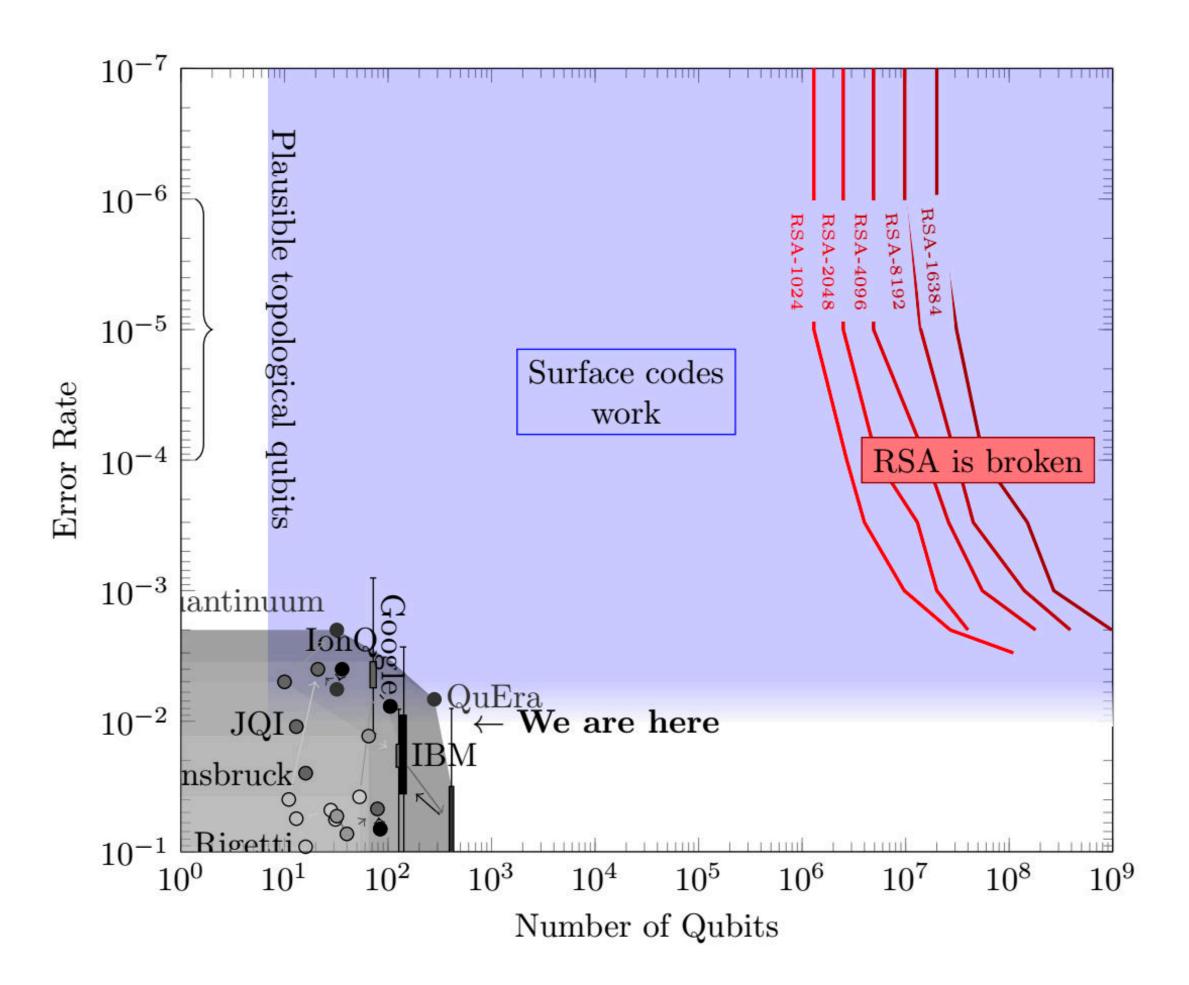


## ...maybe?





## If Microsoft made a topological qubit:

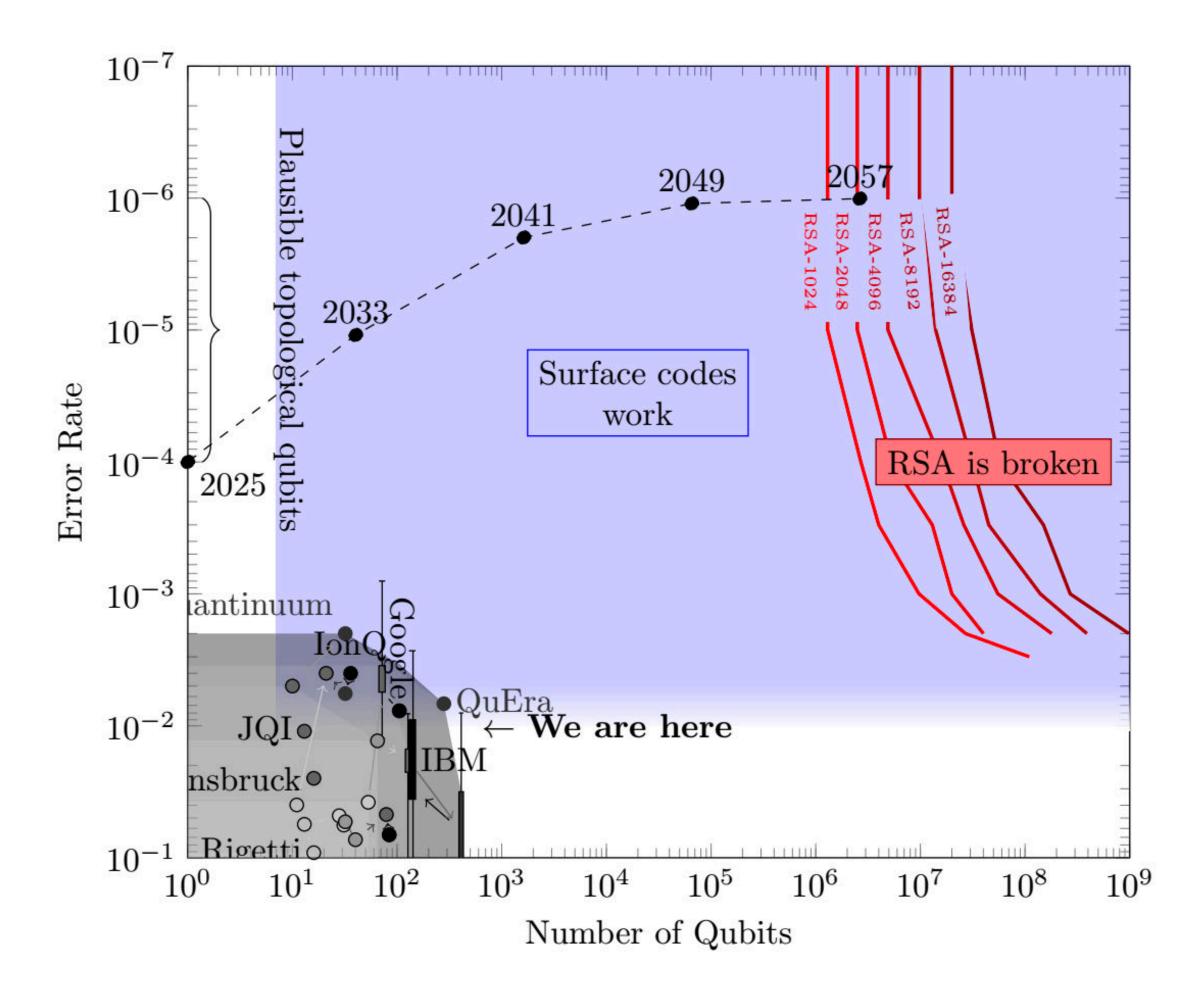


Even Microsoft (arxiv:2211.07629) expects topological qubits to need error correction





## If Microsoft made a topological qubit:

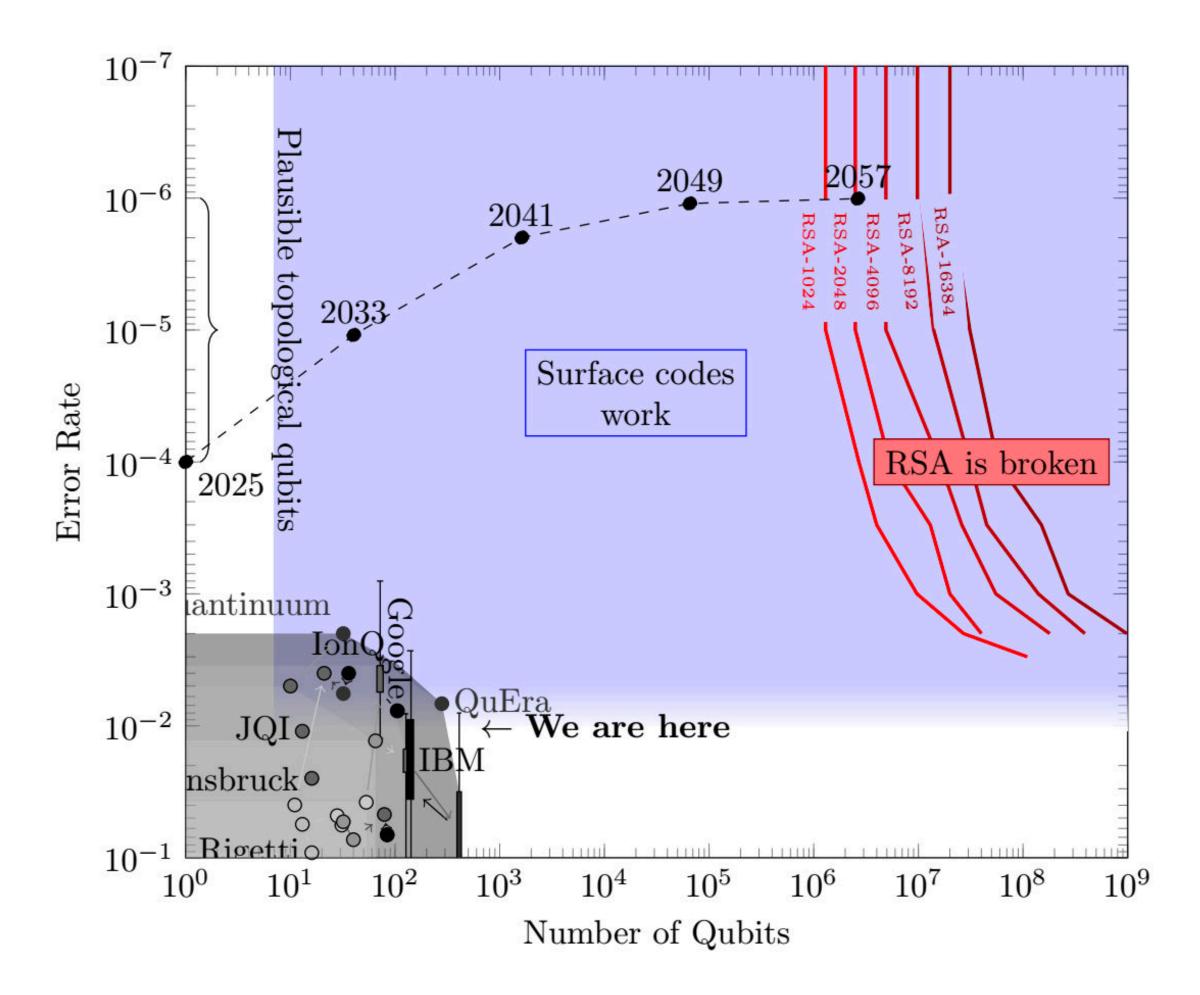


Even Microsoft (arxiv:2211.07629) expects topological qubits to need error correction





## If Microsoft made a topological qubit:



Even Microsoft (arxiv:2211.07629) expects topological qubits to need error correction

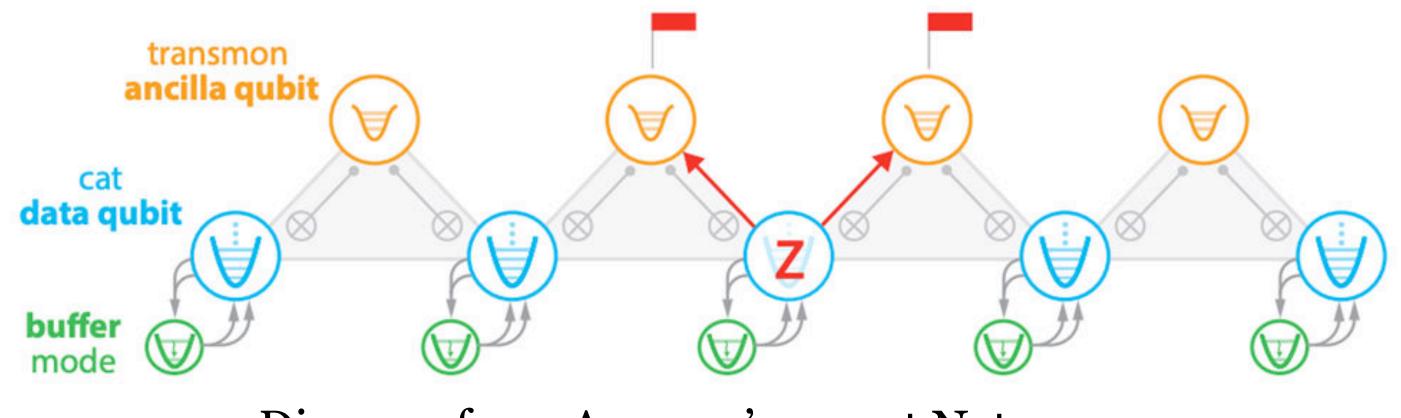
With 18-month doubling it's still a long ways from factoring

Surface codes have a high minimum overhead





## **Cat Qubits**



Quantum computing has two dimension of error: bit flips and phase flips

Cat qubit: each physical qubit is a coherent mixture of many photons, making bit flip errors **exponentially harder** but phase flips **linearly** easier

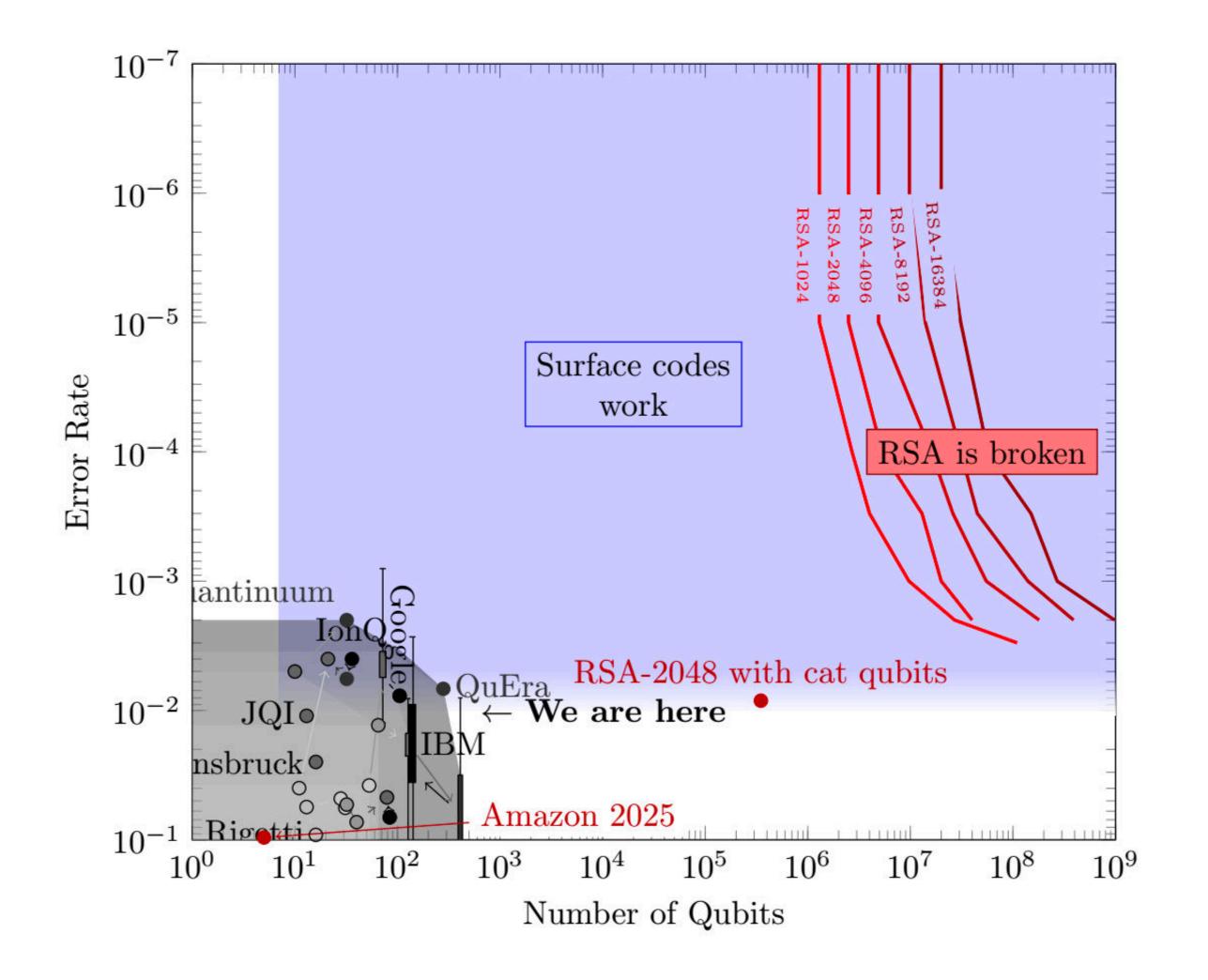
Benefit: can use an unbalanced surface code

Diagram from Amazon's recent Nature paper





## **Cat Qubits**



- "Only" 15 doublings from here (2047 with Moore's law scaling)
  - (18 doublings with superconductors)
- Lots of uncertainties in hardware development

(Resource estimate from Gouzien et al. arxiv:2302.06639)





## My opinions on hardware advances:



Google: "slow and steady" approach: use a more mature technology but which will require large overheads



Microsoft and Amazon: aiming for a riskier technology that might leap ahead

- What to look for:

  - something besides superconductors?

• Will Microsoft irrefutably demonstrate a topological qubit? Will anyone demonstrate surface code error correction with





## 2. Better codes?

- The surface code is a (cohomological) product of two repetition codes: one for bit flip errors, one for phase flips
  - Nearly the simplest code you can construct
- Its asymptotic rate is zero
- Isn't there something better?

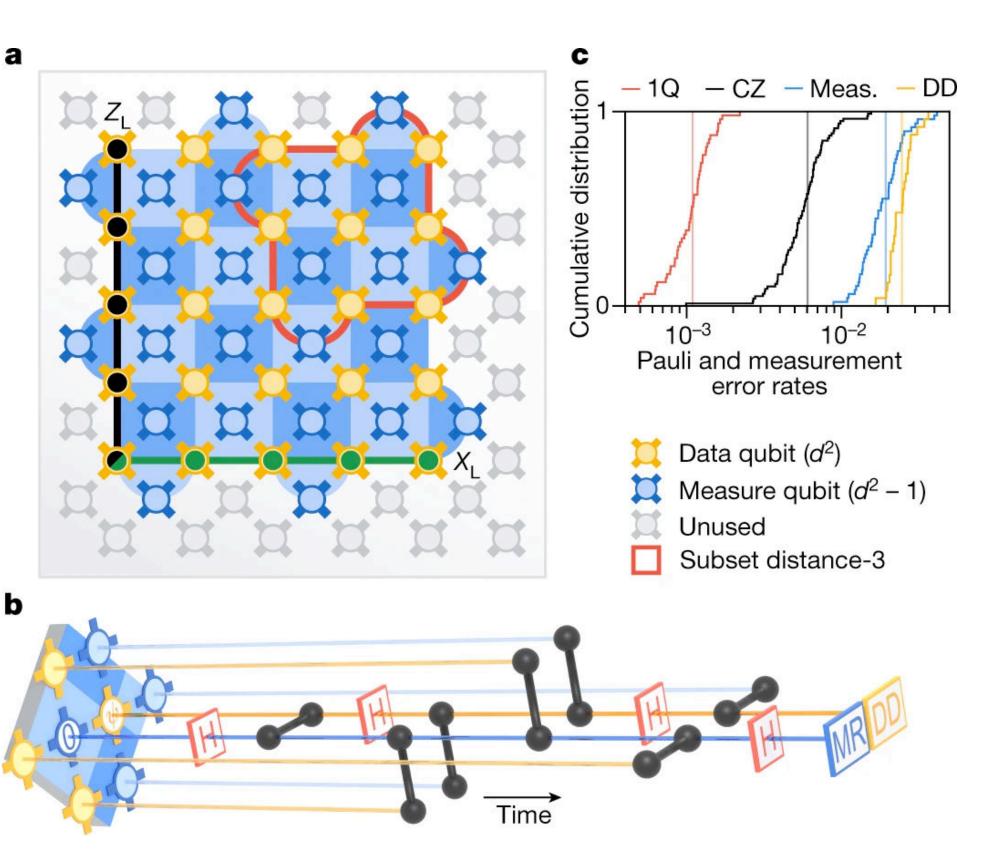


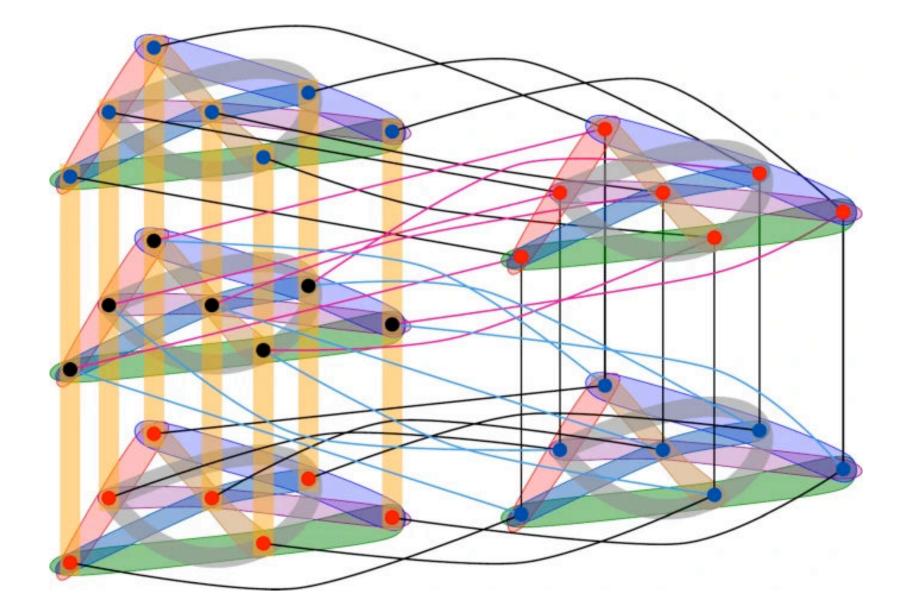
Diagram: Google Quantum AI





## Asymptotically Good Codes

- In 2021 Pantaleev and Kalachev found an LDPC code with a constant ratio of physical:logical qubits
- LDPC = low density parity check, meaning errors can be detected with small circuits
- Physical:logic qubits maybe 14:1
  - Surface code is 881:1

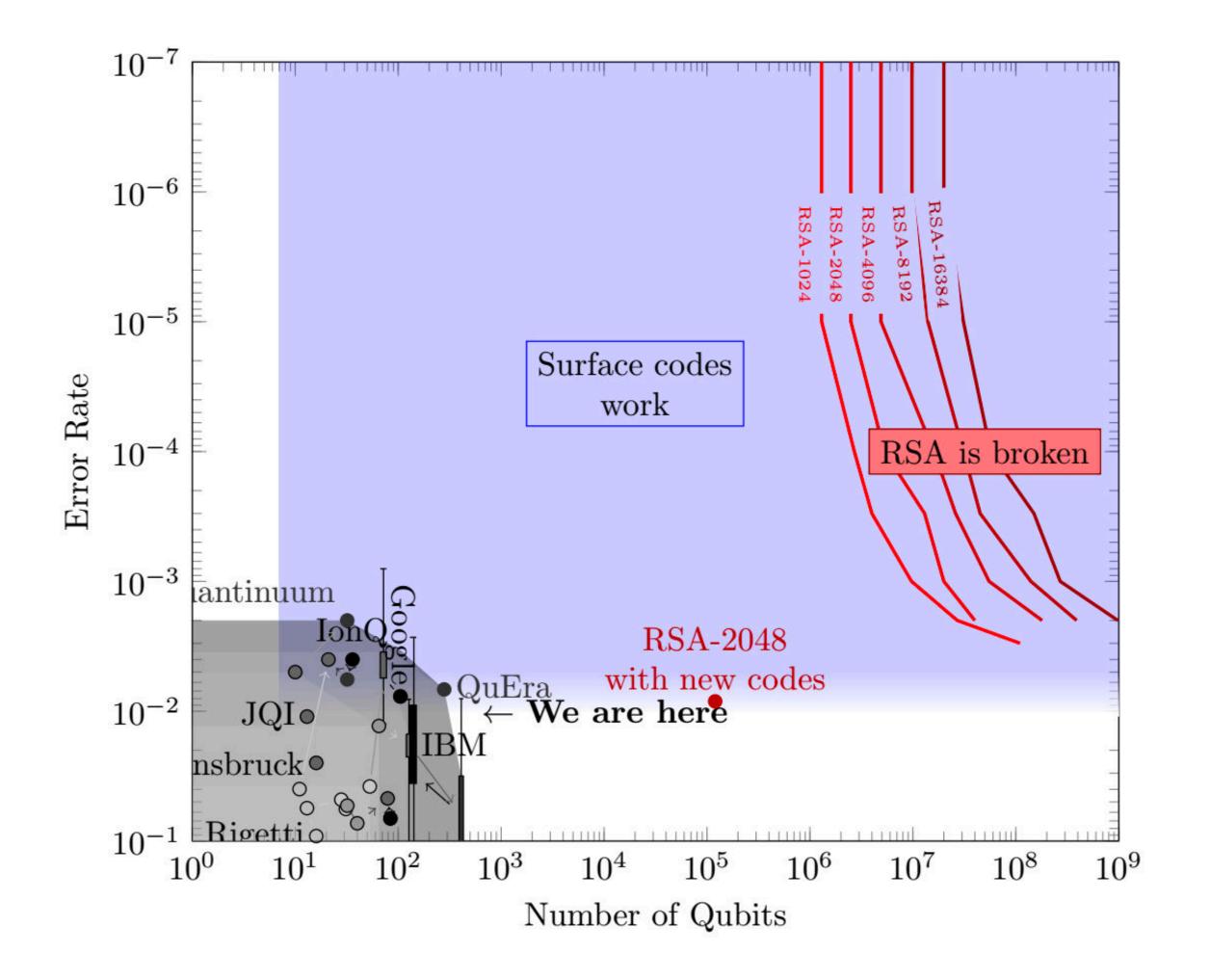


From Akhtar and Marty, 2024. This is just a hypergraph product, a core mathematical building block of these new codes





### Asymptotically good codes



- Only 10 doublings from here (2039 with Moore's law scaling)
- What's the catch?





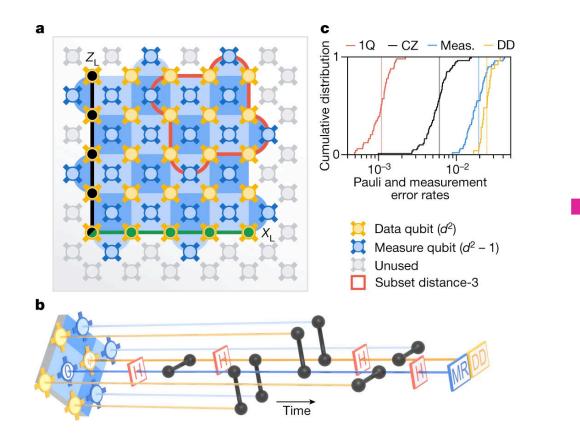
1. Long-range interactions between qubits

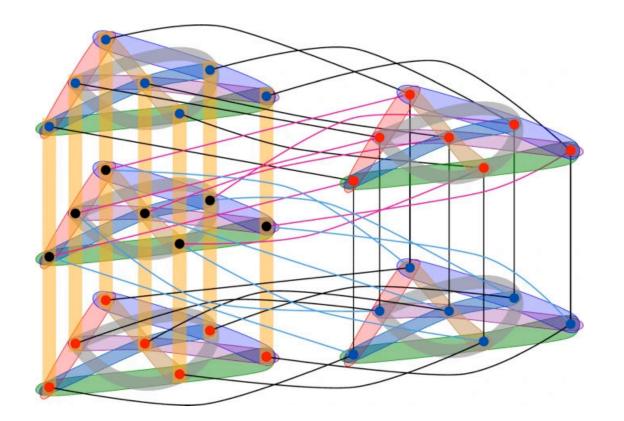
2. Uncertain how to compute with them

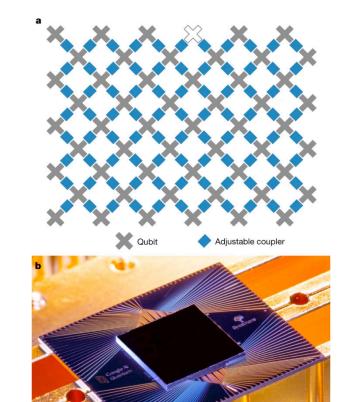




#### 1. Long-range interactions between qubits







#### 5555555

WATERLOO



1. Long-range interactions between qubits

Baspin and Krishna (arXiv:2109.10982) show that long-range interactions **cannot be avoided** for high-rate codes. In fact the surface code is optimal for codes in that layout!

Can any hardware handle long-range interactions? Ion trappers will tell you that ion traps can!

I'm skeptical about scalability



**Products & Solutions** 

Res

What makes our trapped-ion systems so transformative

Realizing the world-changing power of quantum computing will require many qubits, high physical fidelity, and fault tolerance. Our systems have unparalleled fidelity, combined with all-to-all connectivity, mid-circuit measurement, and qubit reuse, giving us an unmatched advantage for pushing the field of quantum computing forward. And the results speak for themselves.

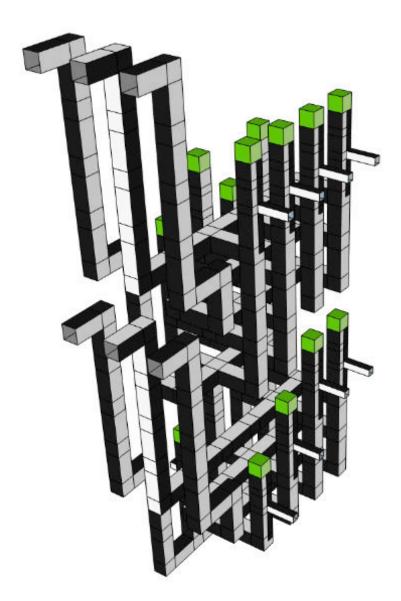


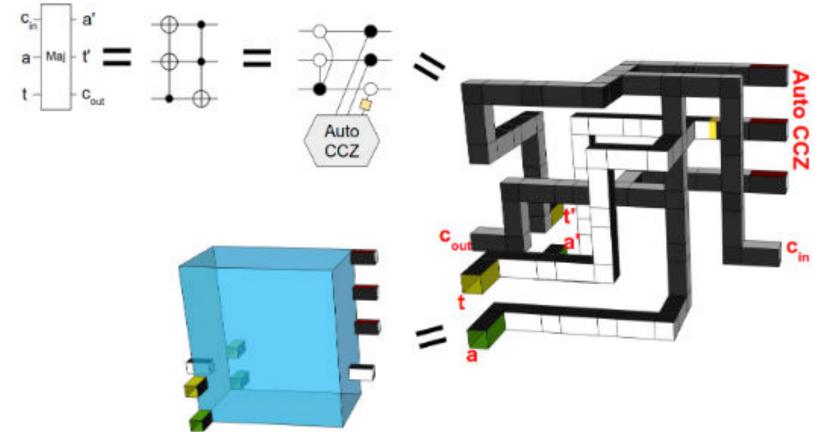


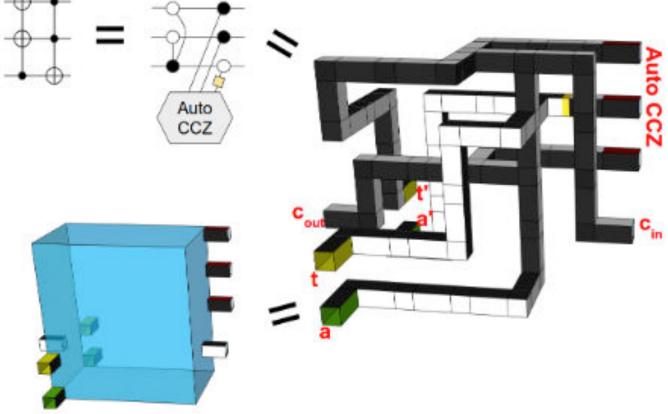
2. Uncertain how to compute with them

Qubits are so noisy they must **stay** encoded during computations

Computing on encoded data is non-trivial! Look at the surface code:







Gidney and Fowler, arxiv:1905.08916

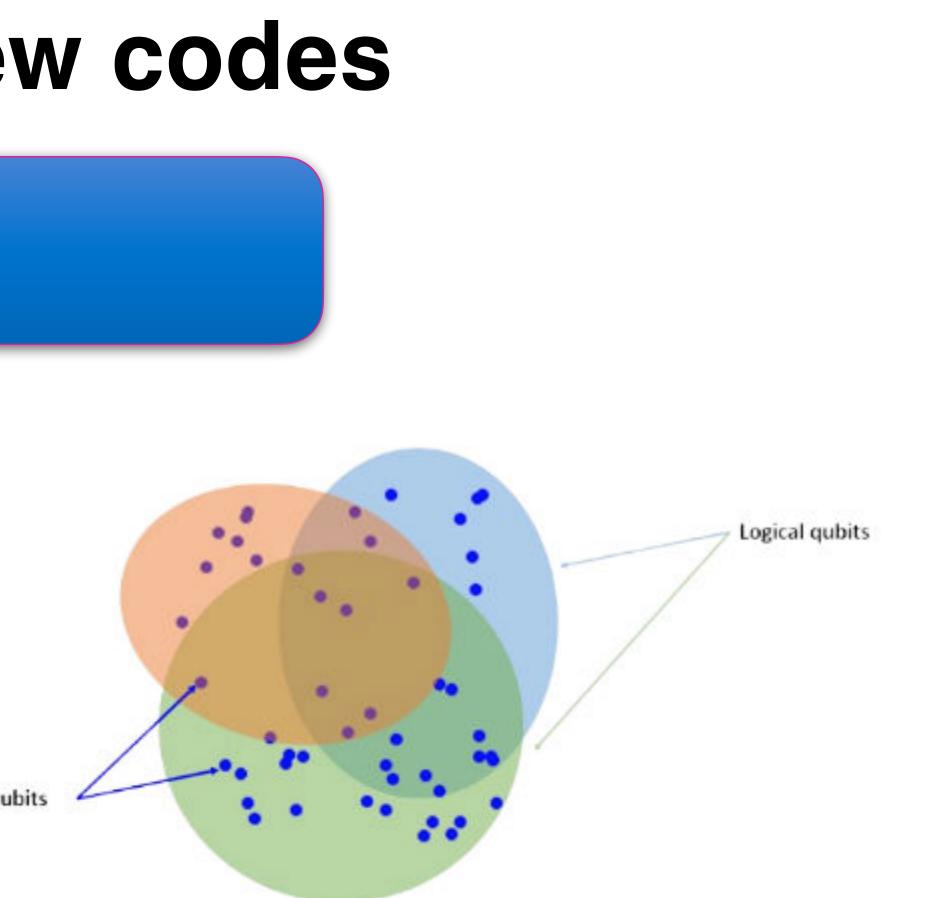




2. Uncertain how to compute with them

Recent results with Jérôme Guyot (arxiv:2502.13889) proved some impossibility results; other recent papers show constructive results in worse codes

Physical qubits







## 3. Better algorithms?

#### In 2021 I wrote:

...Shor's algorithm is mainly just modular exponentiation, meaning that it's about as hard for a quantum computer to *use* RSA as it is to *break* RSA. An asymptotic improvement is highly unlikely





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[Submitted on 12 Aug 2023 (v1), last revised 7 Jan 2024 (this version, v3)]

#### **An Efficient Quantum Factoring Algorithm**

#### **Oded Regev**

We show that *n*-bit integers can be factorized by independently running a quantum circuit with  $\tilde{O}(n^{3/2})$  gates for  $\sqrt{n} + 4$  times, and then using polynomial-time classical post-processing. The correctness of the algorithm relies on a number-theoretic heuristic assumption reminiscent of those used in subexponential classical factorization algorithms. It is currently not clear if the algorithm can lead to improved physical implementations in practice.





## **Regev's New Factoring Algorithm**

From Ekerå and Gärtner (arxiv:2405.14381)

- A.1 RSA IFP
- A.1.1 A basic baseline comparison

		IF	P via	Regev	[30]	with [28,	RSA IFP via Ekerå–Håstad [8, 9, 12]						2]		
						per run	overall					$\mathbf{per}$	run	over	all
$\lceil \log N \rceil$	d	m	C	$\log D$	K	# ops	# ops	m	s	l	n	# ops	adv	# ops	adv
2048	46	50	2.03	96	138	2760	138000	1023	_	993	1	6018	0.46	6018	22.9
									17	61	20	2290	1.20	45800	3.01

- Total gate complexity is still  $O(n^3)$  (like Shor's) but split into  $O(n^{1/2})$  runs
  - Ekerå and Gärtner (arxiv:2311.05545) show that it tolerates runs with errors
  - Overall error correction might be lower, but it remains to be seen

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## **Reducing the Number of Qubits in Quantum Factoring**

Chevignard, Fouque, Schrottenloher (eprint: 2024/222)

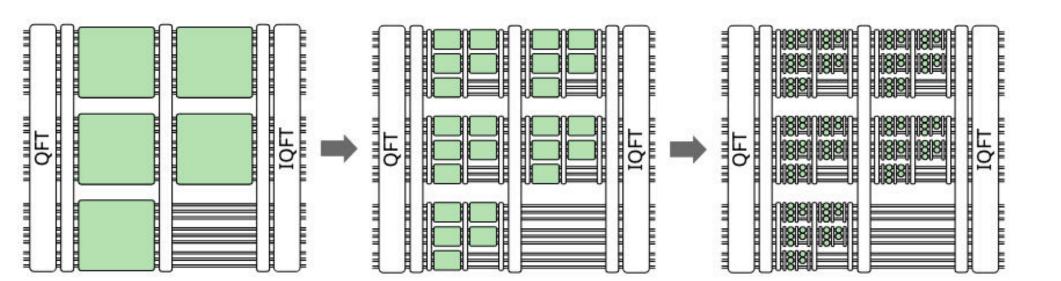
Reduces logical qubit count by using the residue number system

At least 1.6 million physical qubits (likely more for "state factories" and routing)

### Fast quantum integer multiplication with zero ancillas

Kahanamoku-Meyer and Yao (arxiv: 2403.18006)

Uses QFT arithmetic; likely improves in practice but not with the paper above









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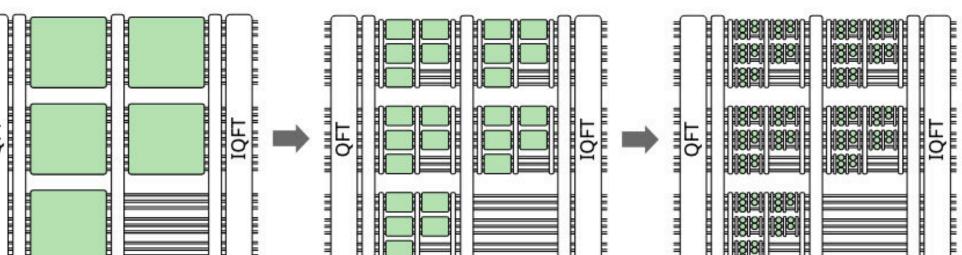
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Overall: great work but I don't expect more than 10x cost reduction, if any



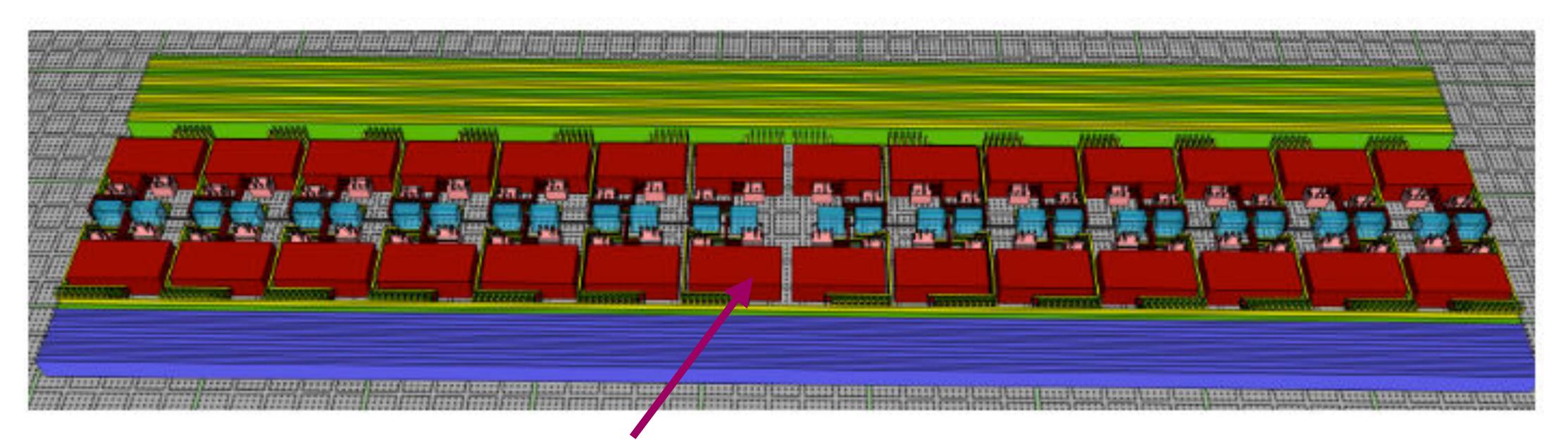






### 4. Better Implementations

Surface code layout for Shor's algorithm from Gidney and Ekerå 2019. Time is vertical axis



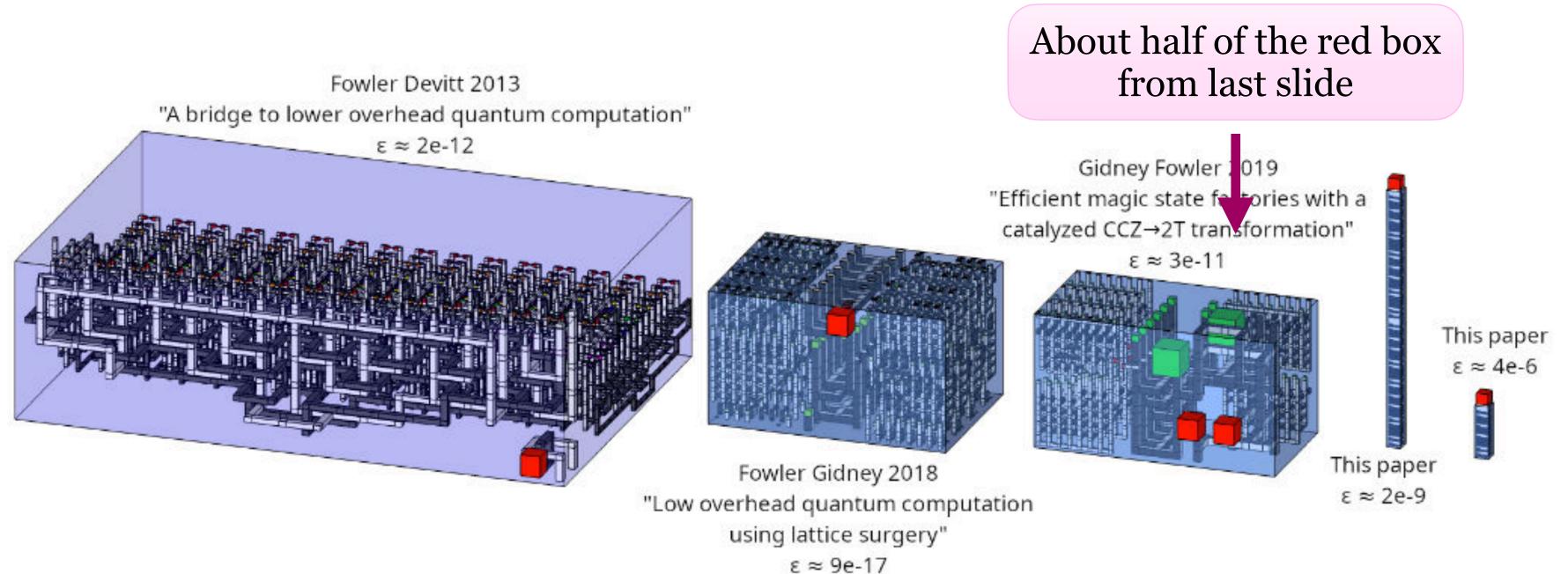
Each of these red and pink pairs of boxes does 1 AND gate





## Magic state cultivation

#### - Gidney, Shutty, and Jones (arxiv: 2409.17595) Figure 3 speaks for itself



Not only could this **drastically** reduce resources of previous circuits, it could up use of new classes of circuits





## **Quantum Resource Estimation Stack**

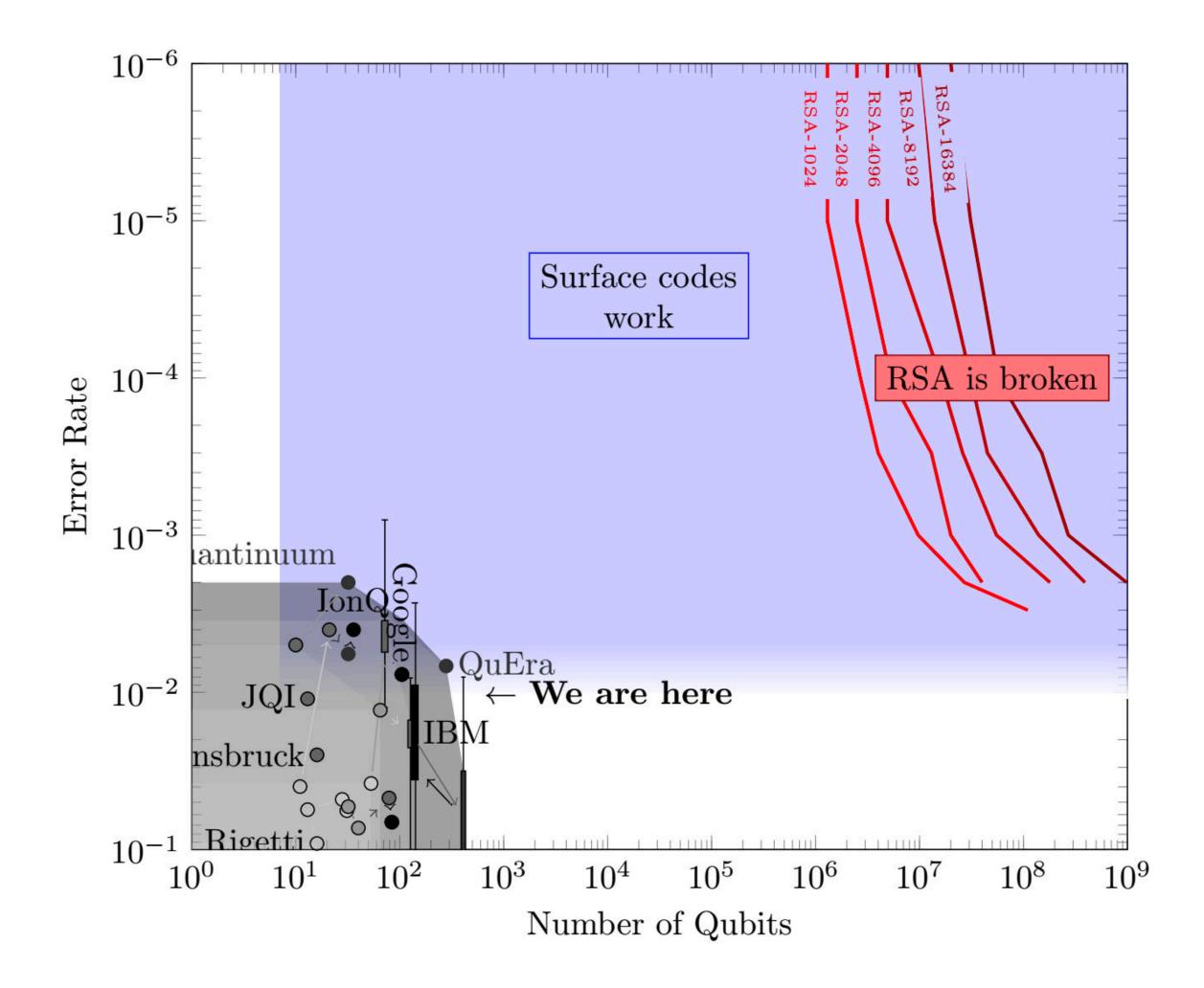
Full-Stack Estimation						
Gidney and Ekerå (2019)	Current State-of-the-art					
Ekerå-Håstad (2017)	Regev (2023)? Chevignard-Fouqe-Schrottenloher (2024)?					
Gidney (2018-2019)	Kahanamoku-Meyer and Yao (2024)?					
Gidney and Ekerå (2019)	??????					
Gidney and Fowler (2019)	Gidney, Shutty, and Jones (2024)					

	Full-Stack Estimation					
	Gidney and Ekerå (2019)	Current State-of-the-art				
Factoring Algorithm	Ekerå-Håstad (2017)	Regev (2023)? Chevignard-Fouqe-Schrottenloher (2024)?				
Arithmetic Circuits	Gidney (2018-2019)	Kahanamoku-Meyer and Yao (2024)?				
Error-corrected layout	Gidney and Ekerå (2019)	??????				
Fault-Tolerant Gates	Gidney and Fowler (2019)	Gidney, Shutty, and Jones (2024)				





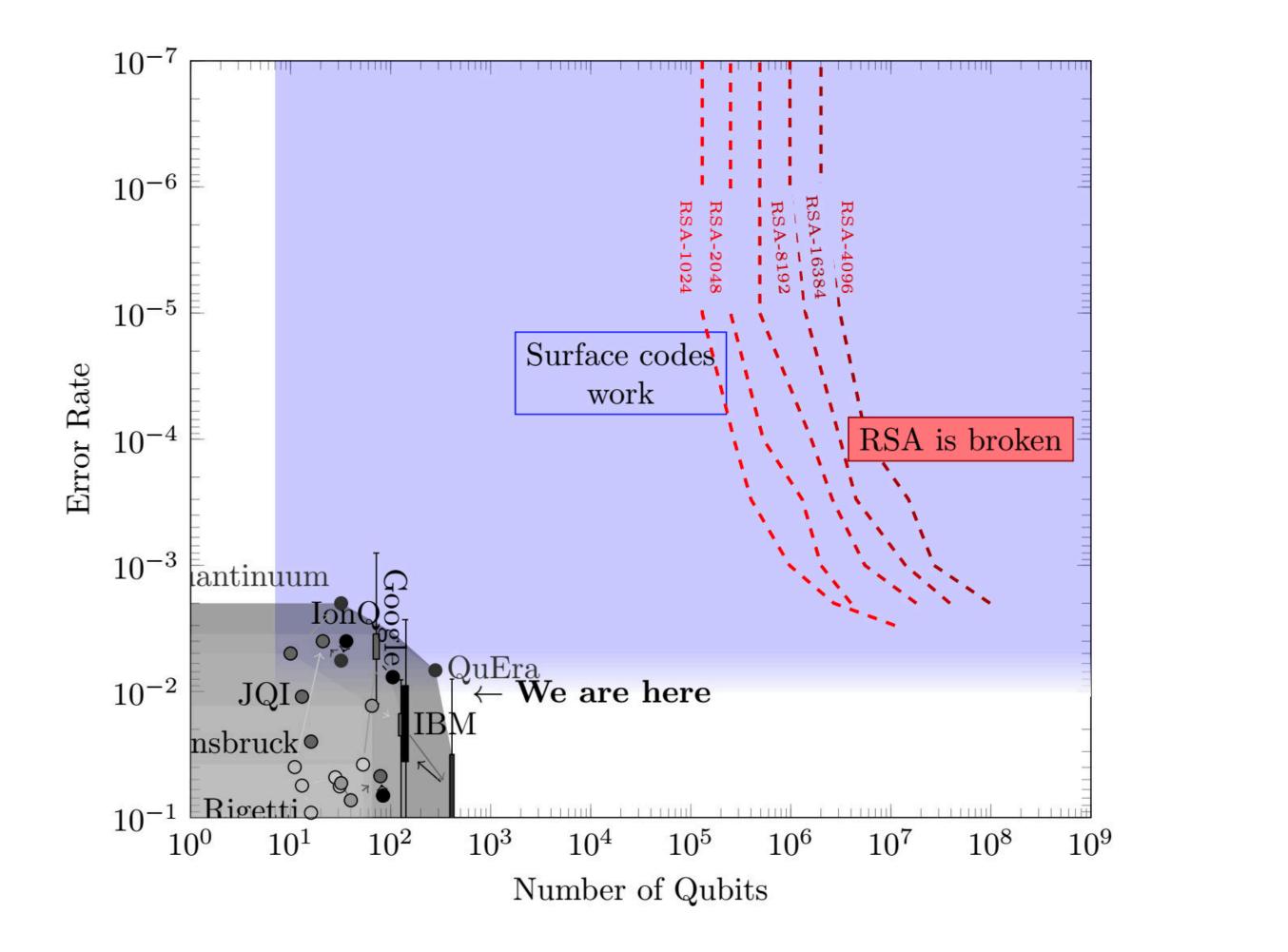
### The chart I would like to show you







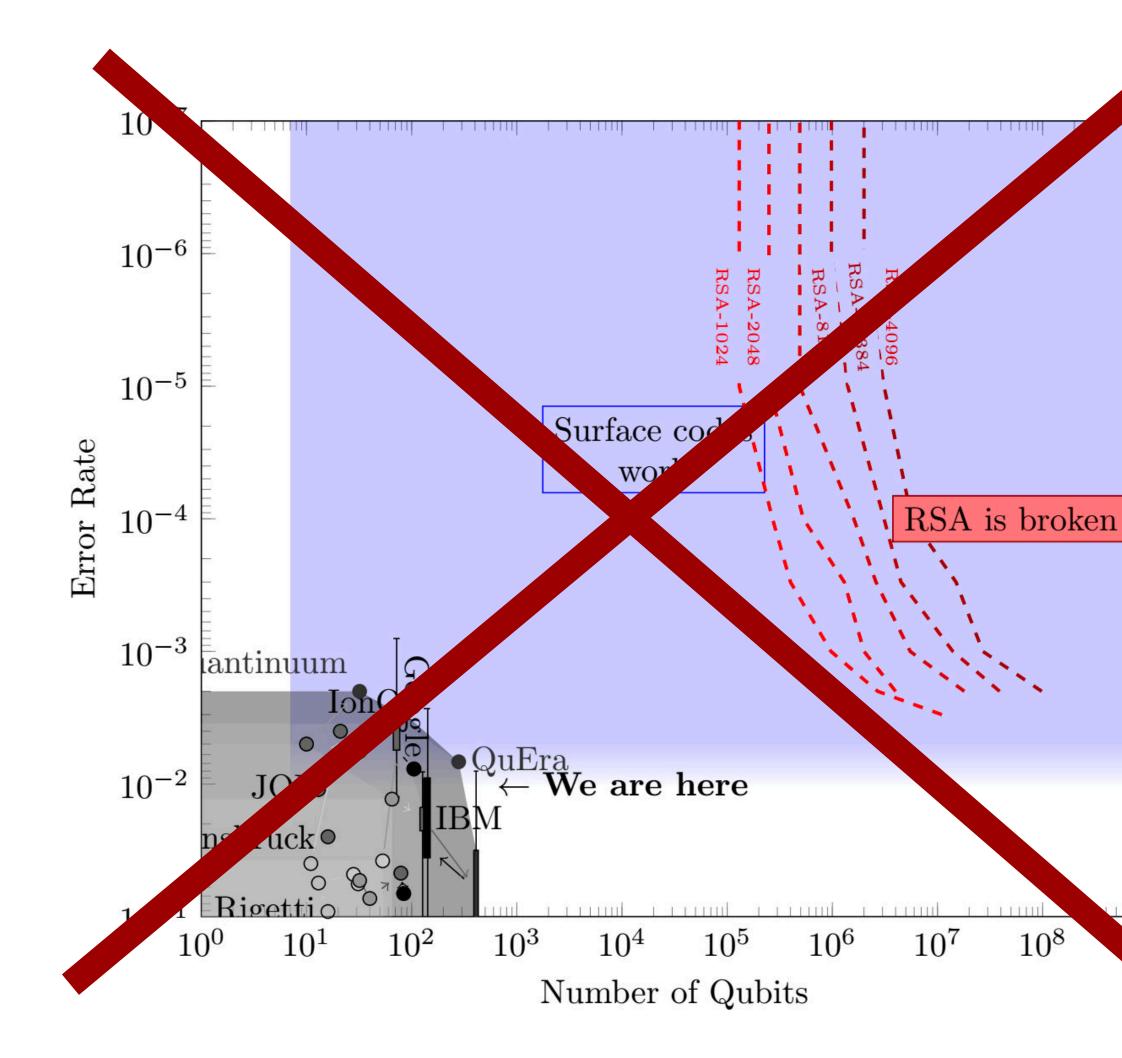
### The chart I would like to show you







## The chart I would like to show you



- The red lines came from a full stack estimate of resources in a surface code, including physical layout, "magic state distillation", etc.
- Updating the full stack is a big project no one has done yet





# CONCLUSIONS

- Qubits will need error correction
- Today's best estimate to factor RSA-2048: 20 million qubits (200,000x beyond today)
- RSA is probably easier to factor than this estimate: stay tuned
- Quantum computing is still an immature technology; expect unexpected developments







# CONCLUSIONS

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- RSA is probably easier to factor than this estimate: stay tuned
- Quantum computing is still an immature technology; expect unexpected developments

Thank you, I'm done talking now

Samuel Jaques



